

Online Identification of key-parameters for Synthetic-Based Calibration with Pyramid WFS

Cedric Taïssir HERITIER

T. Fusco, S. Oberti, B. Neichel, S. Esposito, P.Y. Madec, M. Kasper, C. Verinaud, J. Paufique, M. Le Louan,

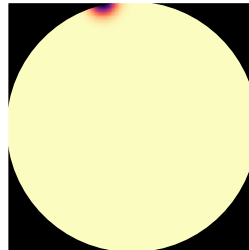


Introduction - AO Calibration

Interaction Matrix D

$=$

How the DM Surface is seen by the WFS



Deformable Mirror (DM)



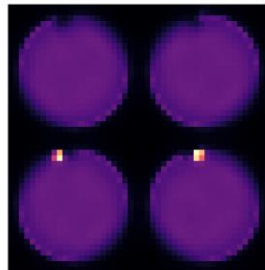
Calibration Source



WFS Measurement Model

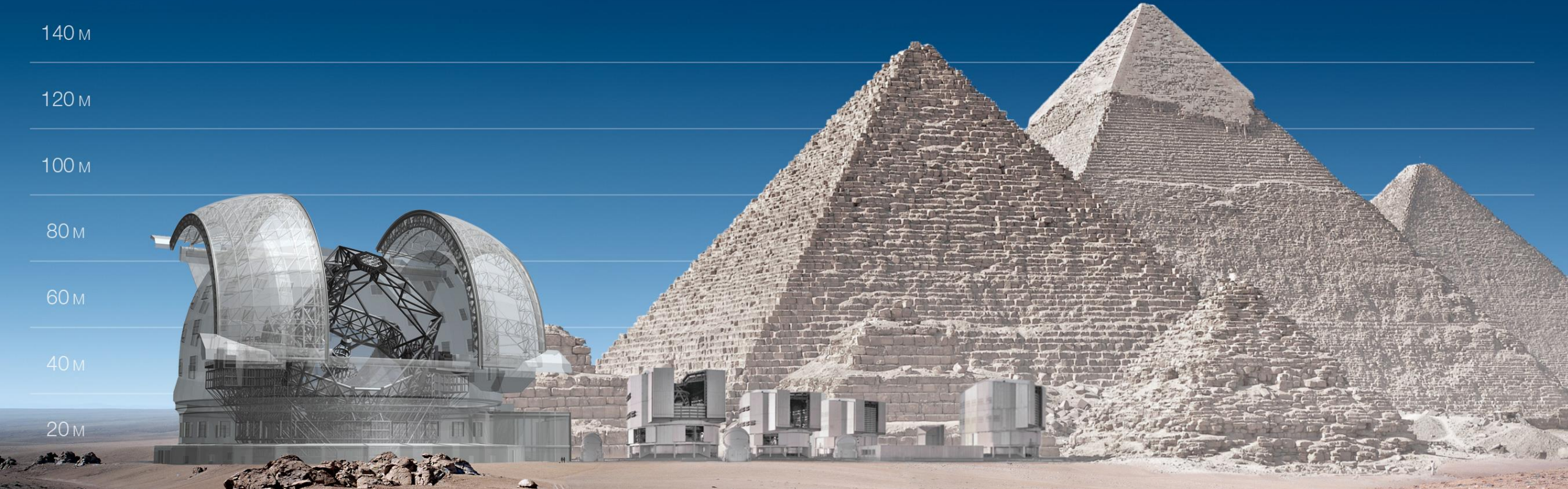
$$D = M_{WFS} \cdot M_{DM}$$

DM Influence Functions



Wave-Front Sensor (WFS)

AO Calibration in the ELT Context



The Future Generation of Telescopes: **The Extremely Large Telescopes**

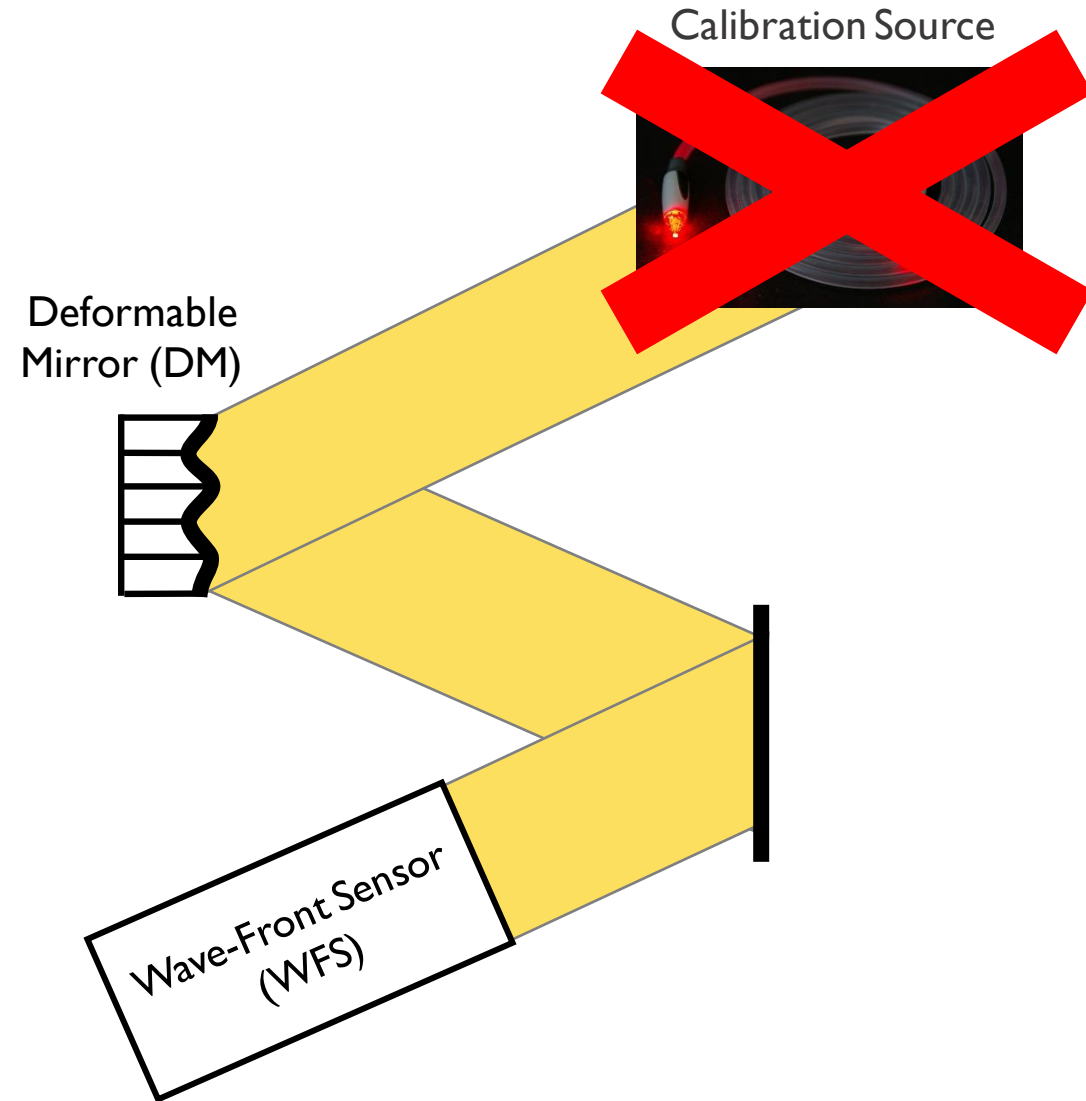
Extremely Large Telescope – 39 m diameter

Giant Magellan Telescope – 24.5 m diameter

Thirty Meter Telescope – 30 m diameter

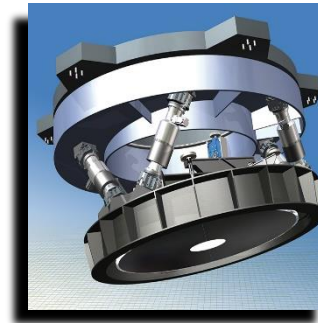
AO Calibration in the ELT Context

- No External Calibration Source
- ...



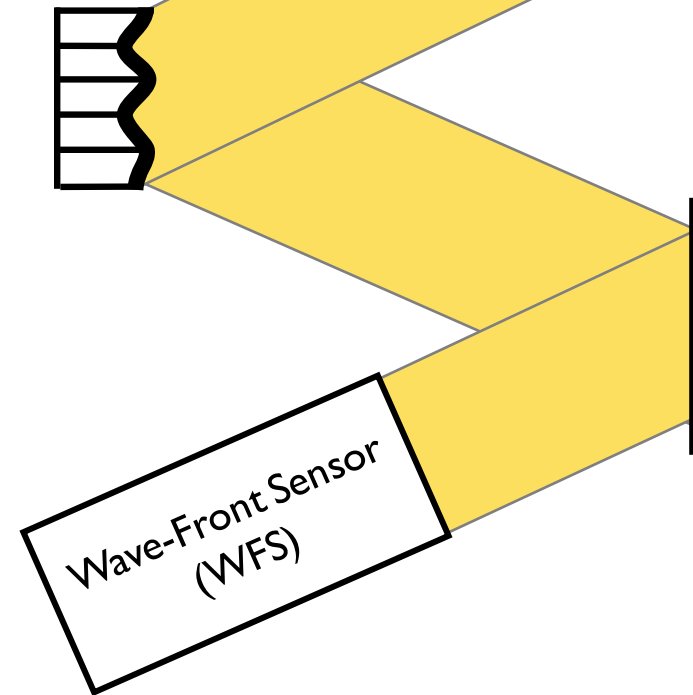
AO Calibration in the ELT Context

- No External Calibration Source
- ~ 5000 Actuators DM
- ...



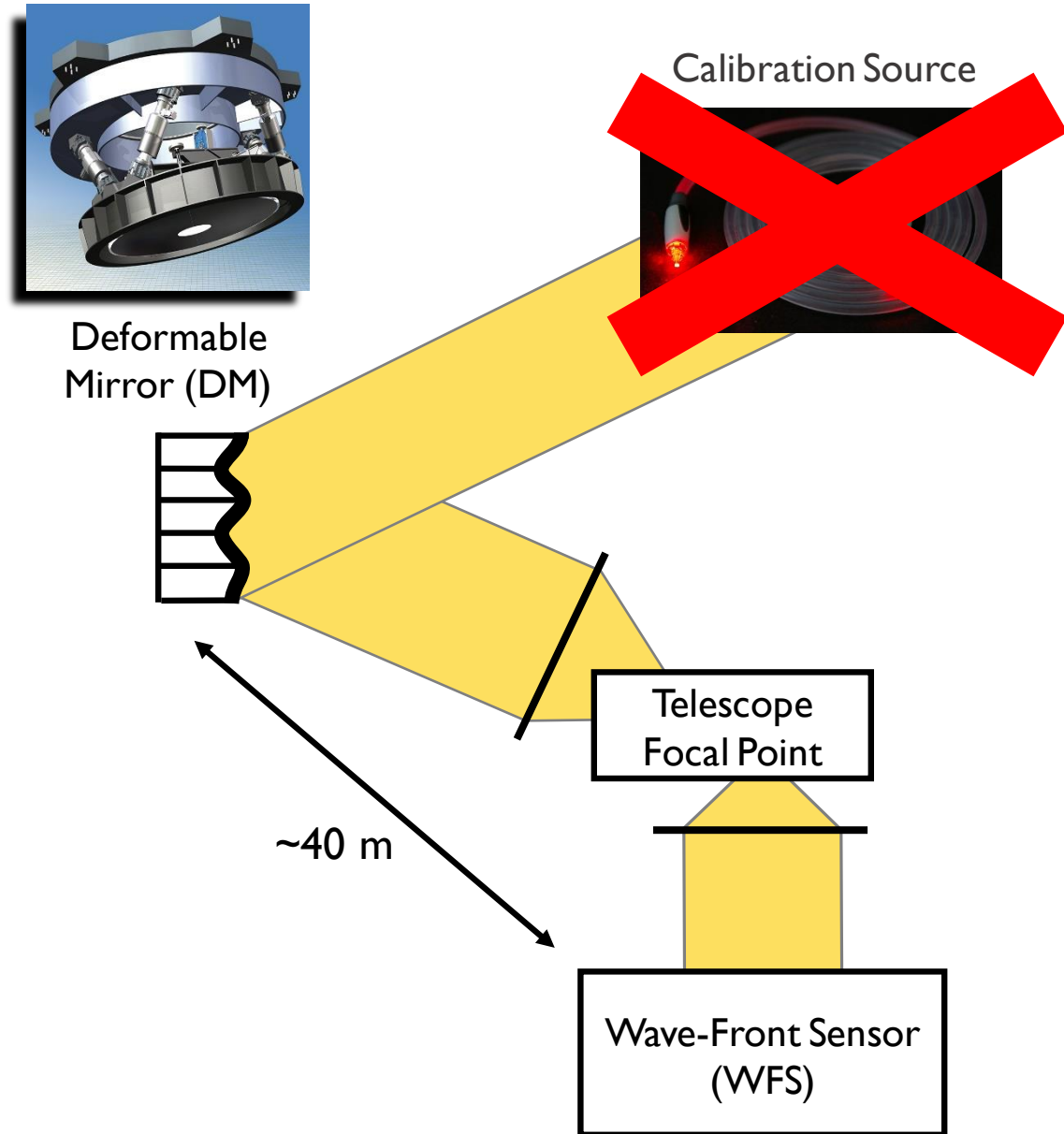
Deformable Mirror (DM)

Calibration Source



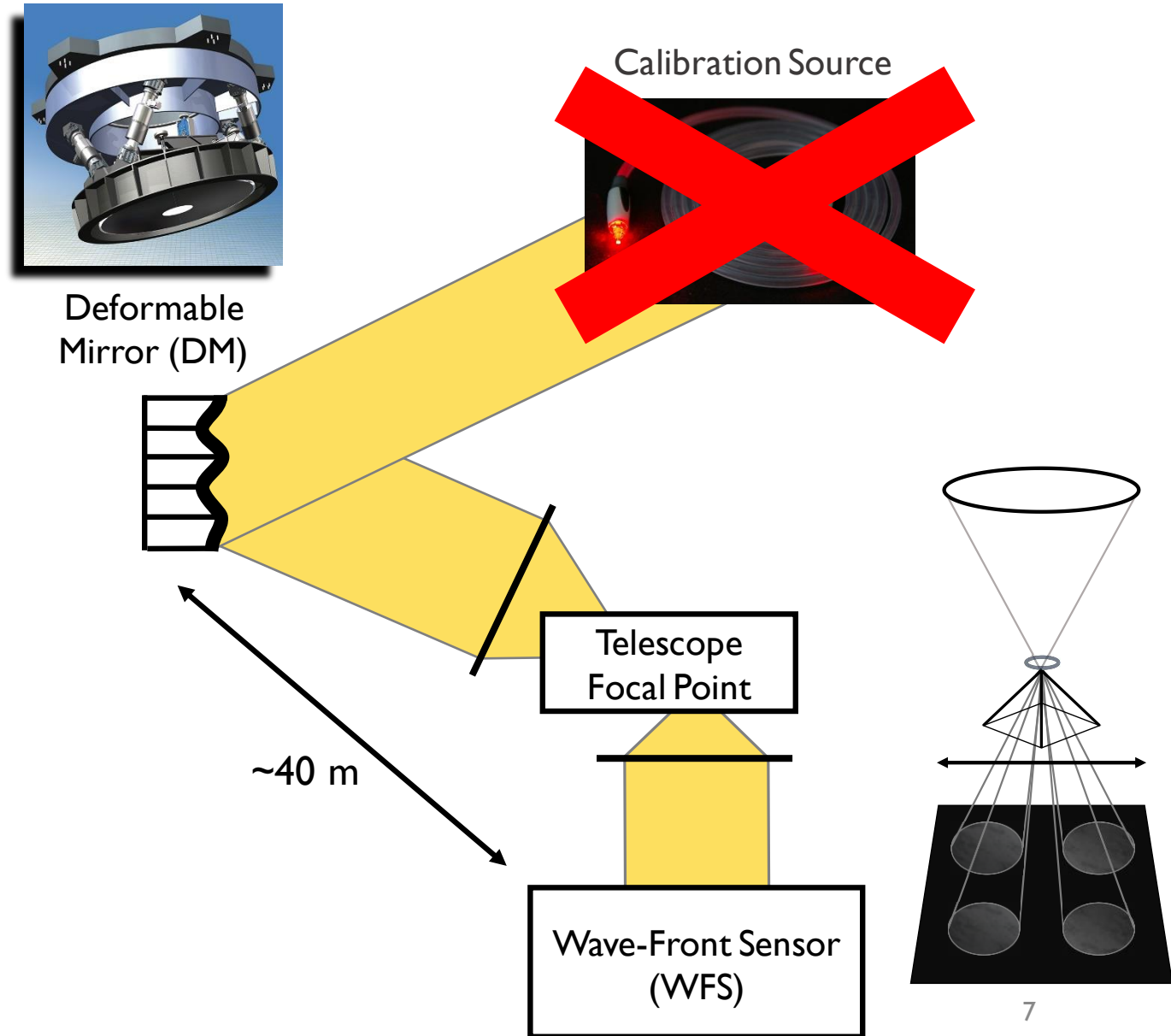
AO Calibration in the ELT Context

- No External Calibration Source
- ~ 5000 Actuators DM
- DM located inside the telescope
- ...



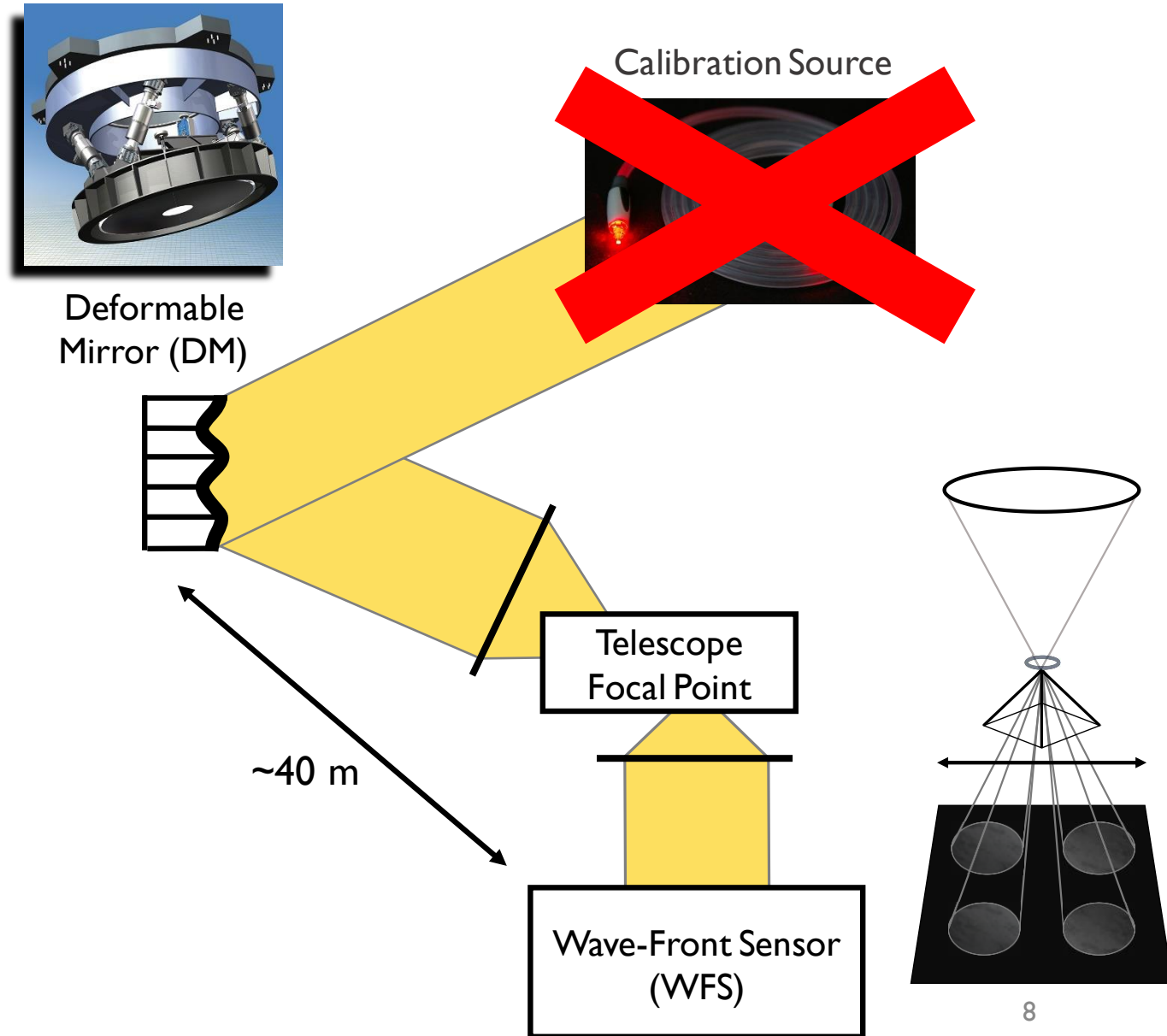
AO Calibration in the ELT Context

- No External Calibration Source
- ~ 5000 Actuators DM
- DM located inside the telescope
- Pyramid WFS Specificities
- ...



AO Calibration in the ELT Context

- No External Calibration Source
- ~ 5000 Actuators DM
- DM located inside the telescope
- Pyramid WFS Specificities
- **Minimize impact on Science**



AO Calibration in the ELT Context

Post Focal AO System



AO Calibration in the ELT Context

Large Adaptive Telescope



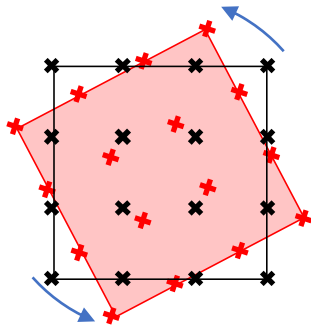
AO Calibration in the ELT Context

Large Adaptive Telescope

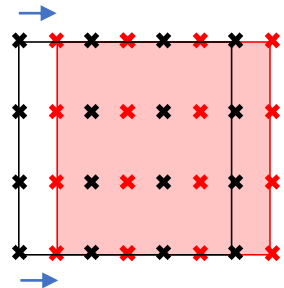


Mis-Registrations

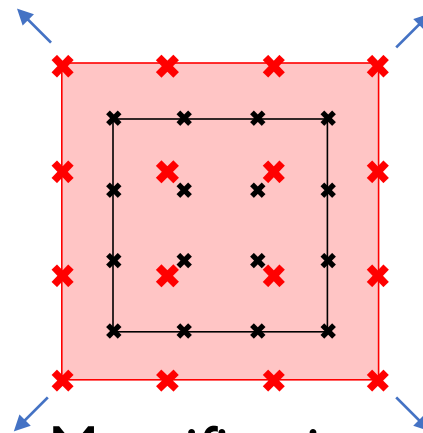
Evolution the DM Actuator grid image as seen by to the WFS.



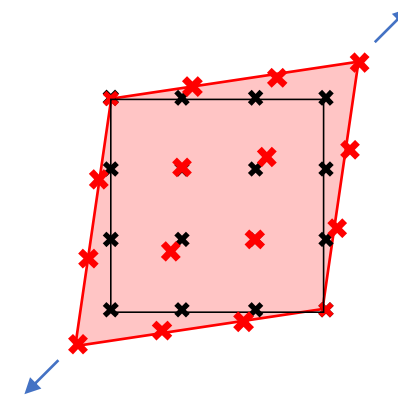
Rotation



Shifts



Magnification

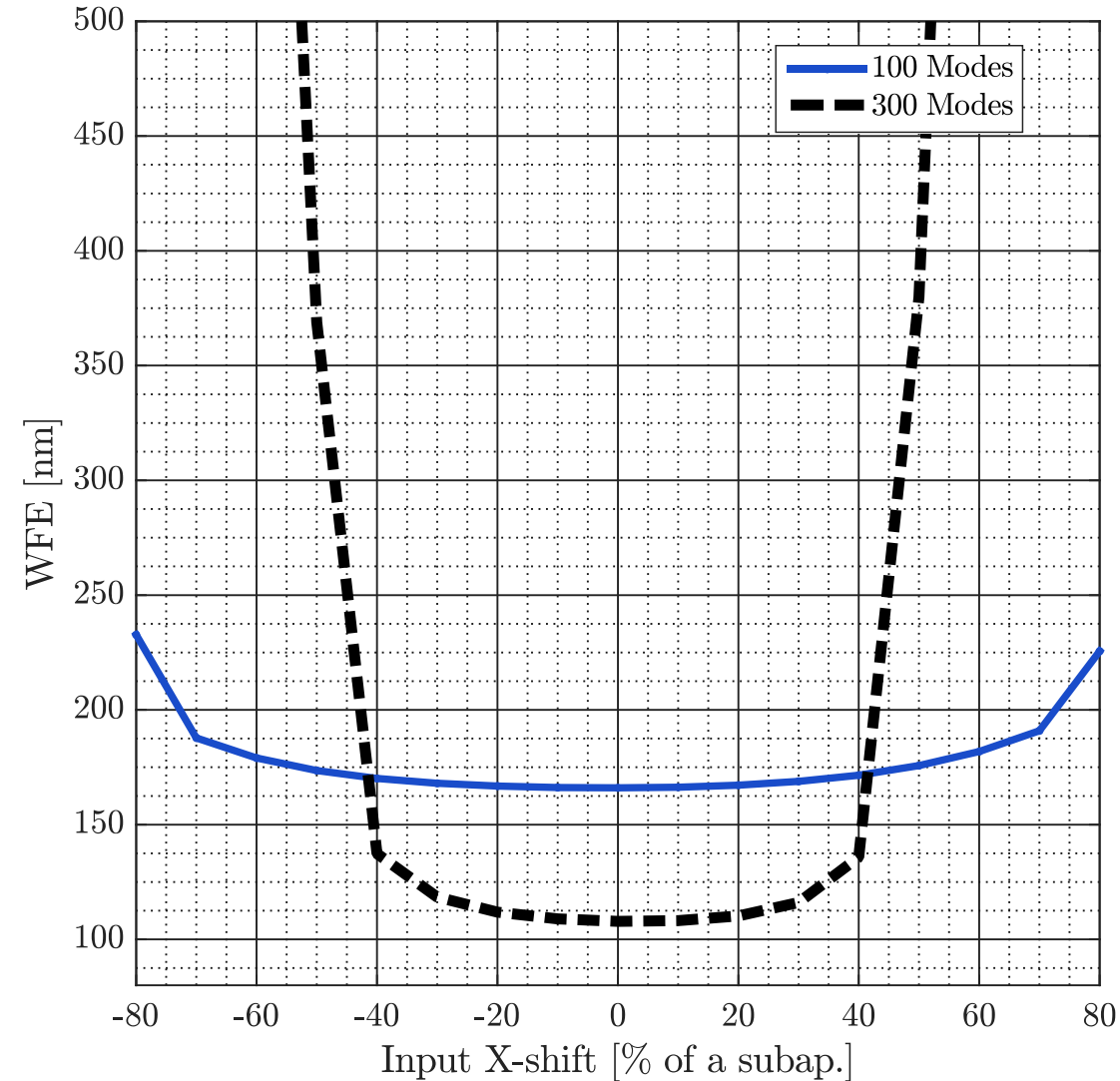


Anamorphosis

I - Impact of a Mis-Registration

- ⇒ Dramatic impact on the AO Correction
- ⇒ Loss of Performance
- ⇒ Loop instability

Monitoring and Compensation of the Mis-Registrations is **necessary!**



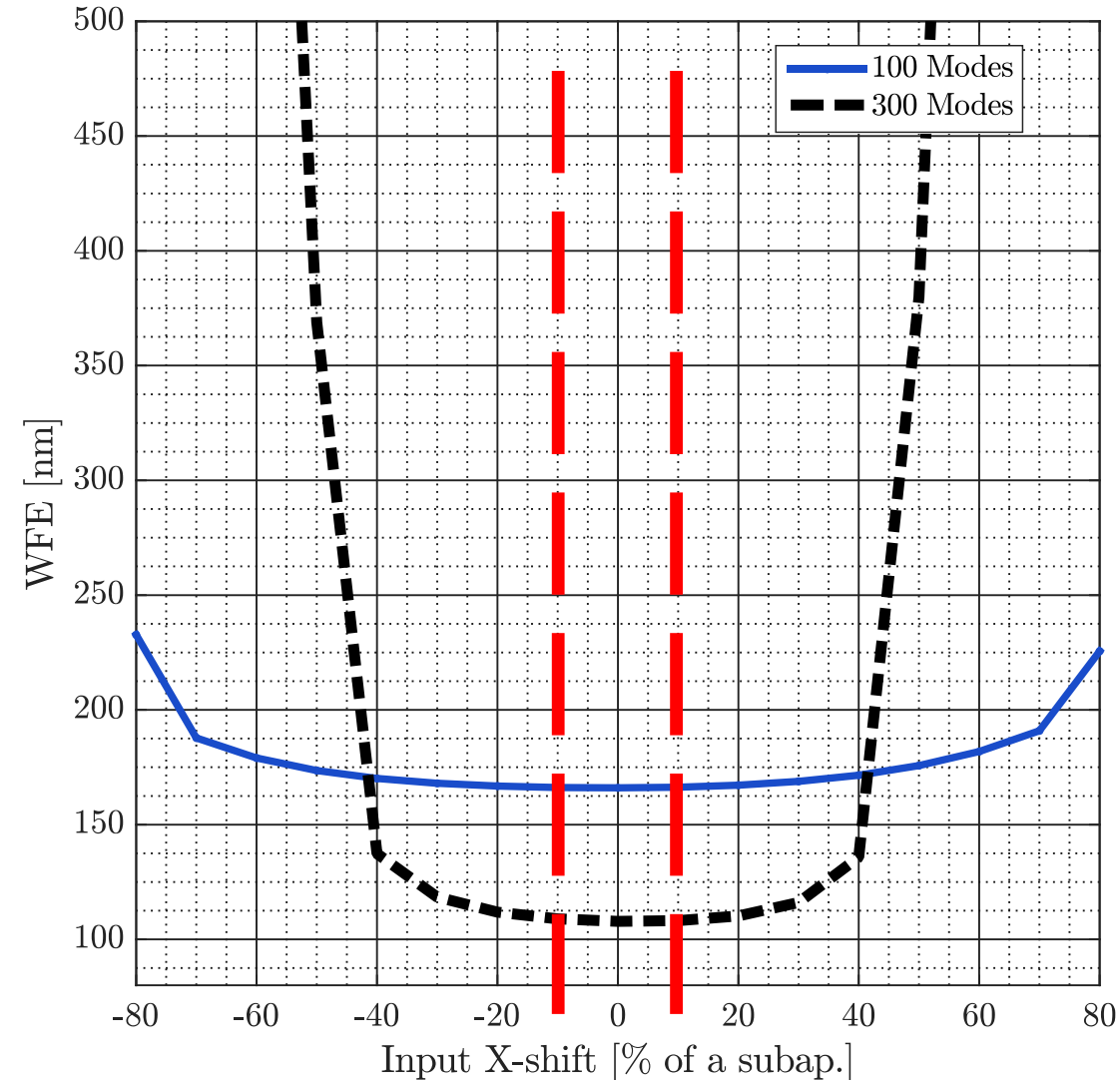
I - Impact of a Mis-Registration

- ⇒ Dramatic impact on the AO Correction
- ⇒ Loss of Performance
- ⇒ Loop instability

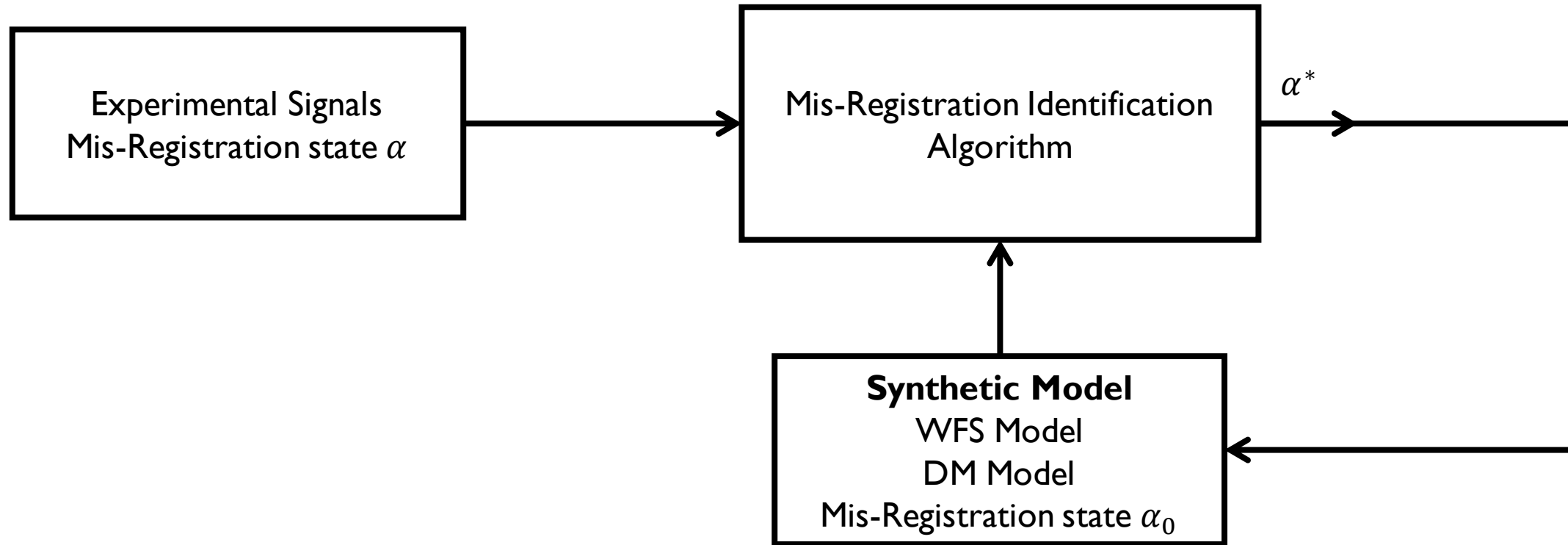
Monitoring and Compensation of the Mis-Registrations is **necessary!**

Typically:

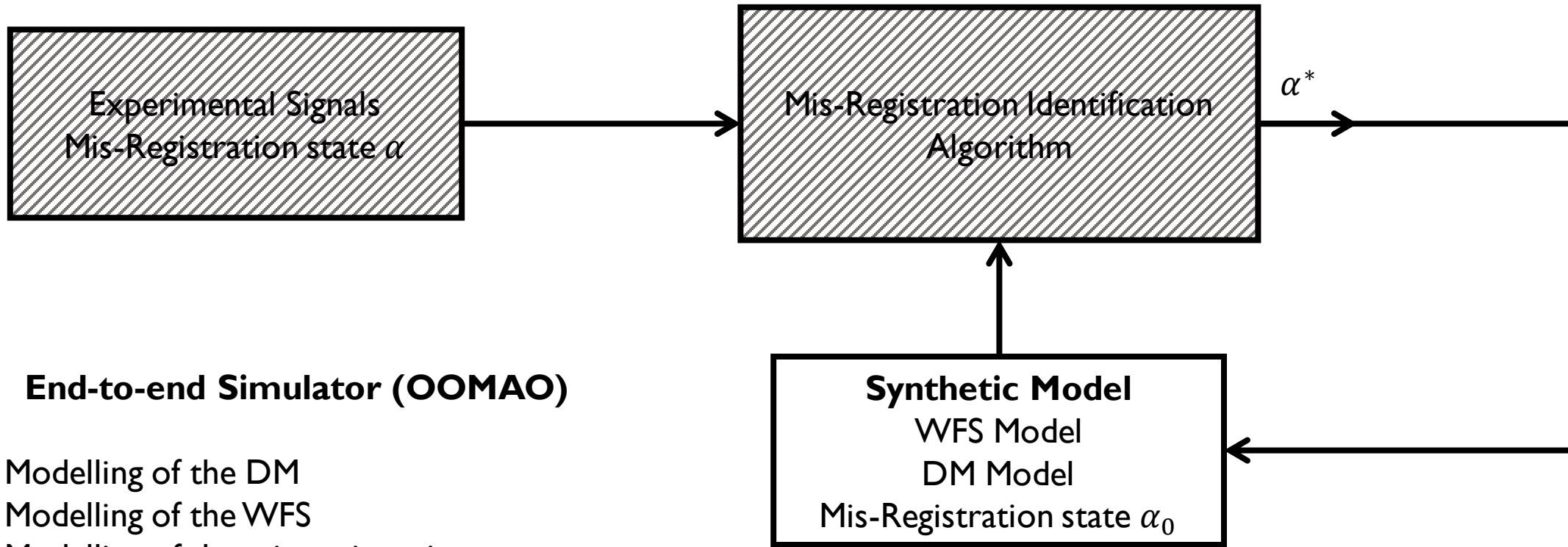
Accuracy < 10% of a subaperture
(System dependent)



Pseudo Synthetic Interaction Matrix



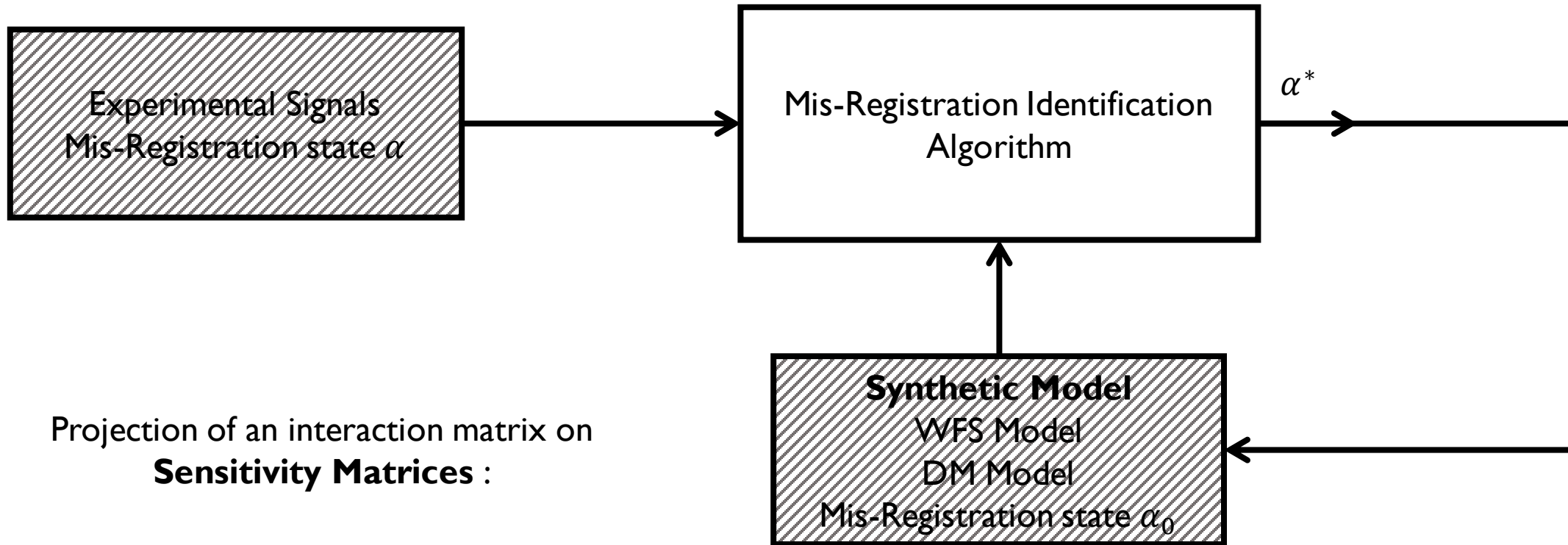
Pseudo Synthetic Interaction Matrix



End-to-end Simulator (OOMAO)

- Modelling of the DM
- Modelling of the WFS
- Modelling of the mis-registrations α

Pseudo Synthetic Interaction Matrix

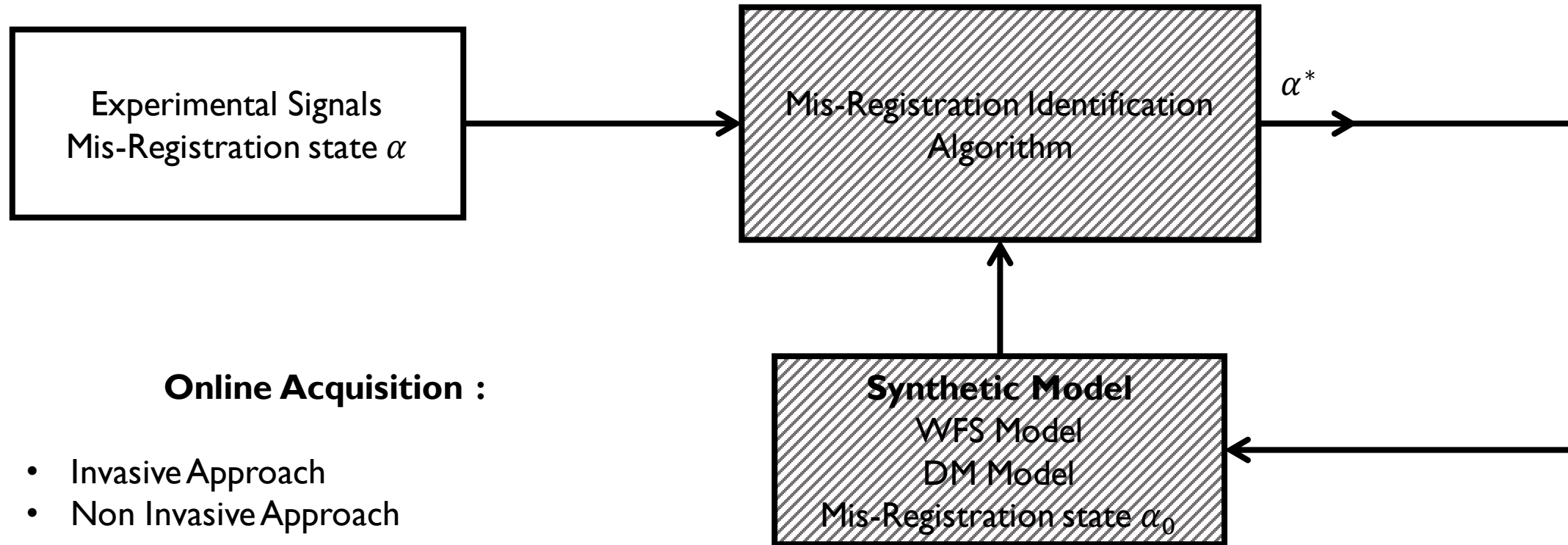


Projection of an interaction matrix on
Sensitivity Matrices :

$$\delta \mathbf{D}_{\alpha_0}(\varepsilon_i) = \frac{\mathbf{D}_{\alpha_0 + \varepsilon_i} - \mathbf{D}_{\alpha_0 - \varepsilon_i}}{2\varepsilon_i}$$

α_0 = Mis-Registration State
 ε_i = "delta" mis-registration

Pseudo Synthetic Interaction Matrix



Online Acquisition :

- Invasive Approach
- Non Invasive Approach

An Invasive Approach - Principle

Principle:

Dithering of a few **well selected modes** to retrieve the mis-registrations parameters.

How?

- Fast Push-Pull? Temporal and Spatial modulation?
- SNR required? Time allocated?
- Impact on the science?

Wildi et al. 2004, Esposito et al. 2006,
Oberti et al. 2006, Pieralli et al. 2008,
Pinna et al. 2012, Kellerer et al. 2012

An Invasive Approach - Principle

Principle:

Dithering of a few **well selected modes** to retrieve the mis-registrations parameters.

How?

- **Fast Push-Pull?** Temporal and Spatial modulation?
- SNR required? Time allocated?
- Impact on the science?

Wildi et al. 2004, Esposito et al. 2006,
Oberti et al. 2006, Pieralli et al. 2008,
Pinna et al. 2012, Kellerer et al. 2012

An Invasive Approach - Principle

Principle:

Dithering of a few **well selected modes** to retrieve the mis-registrations parameters.

How?

- **Fast Push-Pull?** Temporal and Spatial modulation?
- SNR required? Time allocated?
- Impact on the science?

What Signals?

- Spatial properties of the signals?
- Impact on the science?

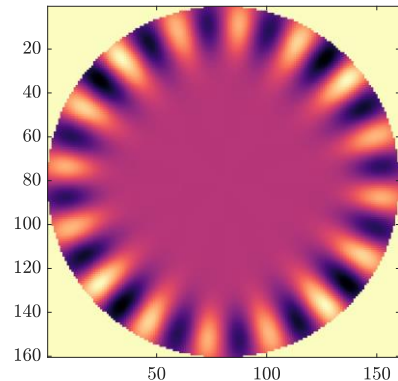
An Invasive Approach - Choice of the signals

Identifying the optimal set of modes to **maximize the sensitivity to a given mis-registration** and minimize the number of modes required.

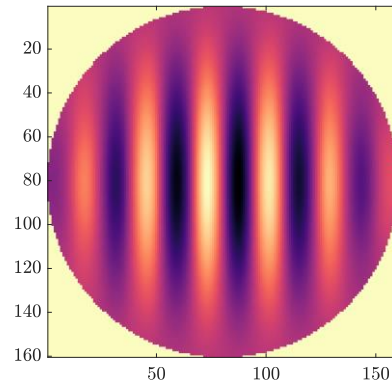
⇒ Principal Component Analysis of the **Sensitivity Matrix**

Ex: 20 by 20 subapertures - Cartesian DM with PWFS:

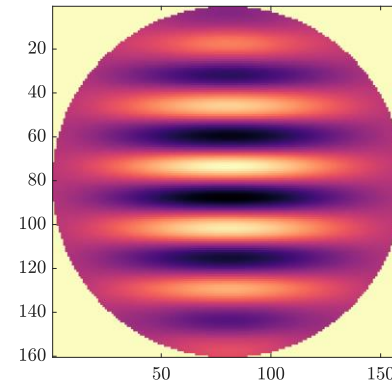
Rotation



Shift X



Shift Y



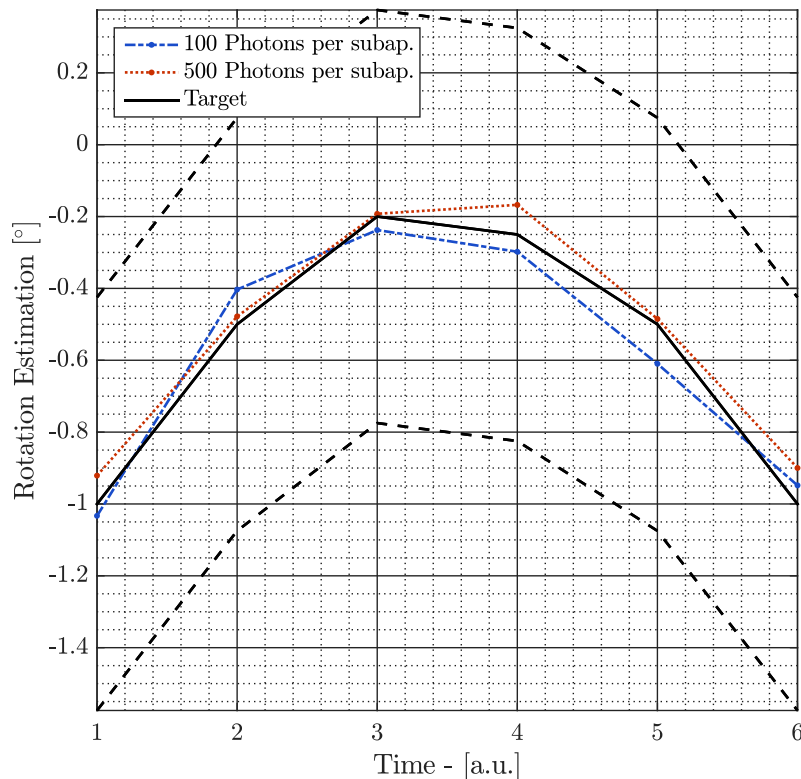
An Invasive Approach - Application

Application: Dynamical tracking of multiple parameters evolving at the same time

20 Fast push-pull of 3 modes - 20 nm RMS

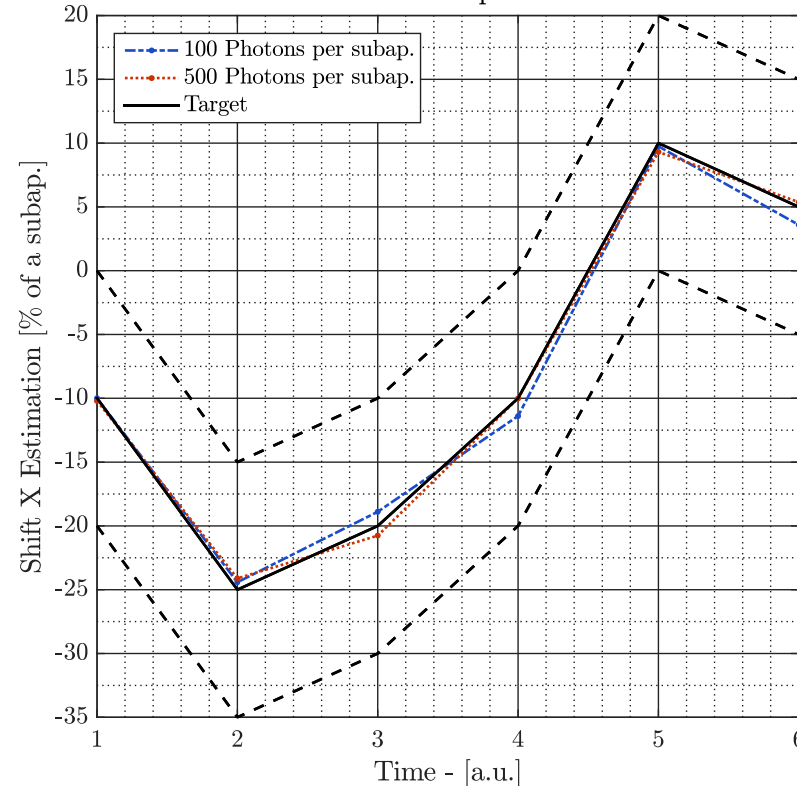
Rotation

3 PCA Modes - Amplitude: 20 nm



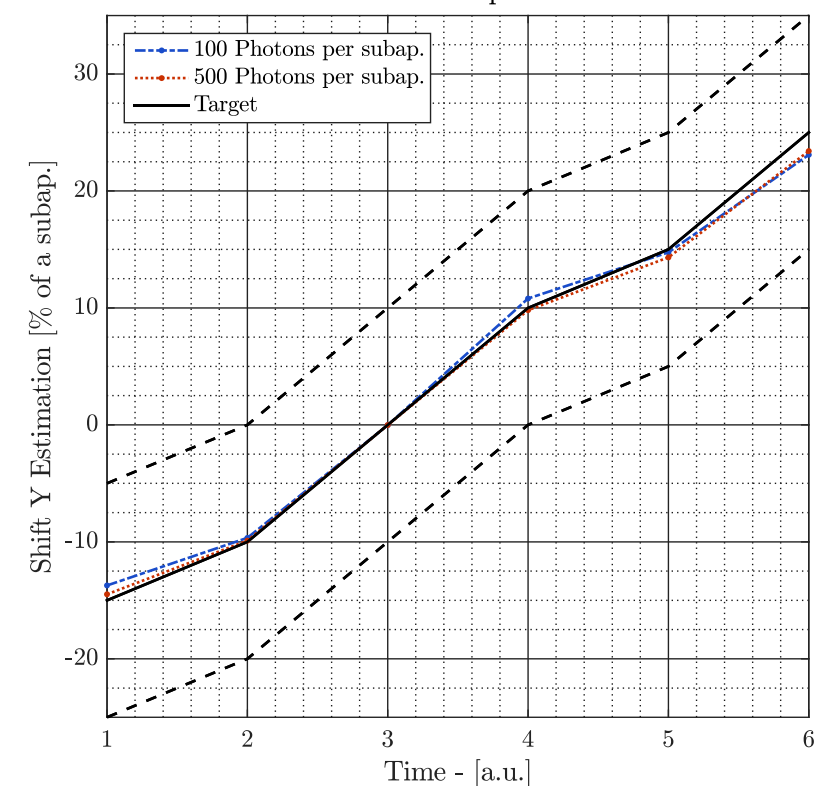
Shift X

3 PCA Modes - Amplitude: 20 nm



Shift Y

3 PCA Modes - Amplitude: 20 nm



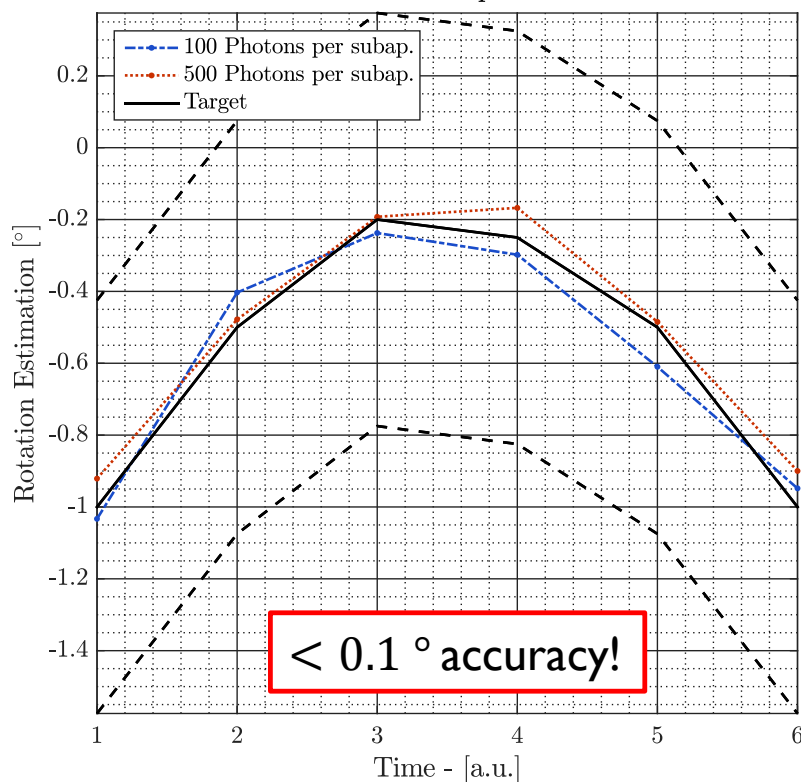
An Invasive Approach - Application

Application: Dynamical tracking of multiple parameters evolving at the same time

20 Fast push-pull of 3 modes - 20 nm RMS

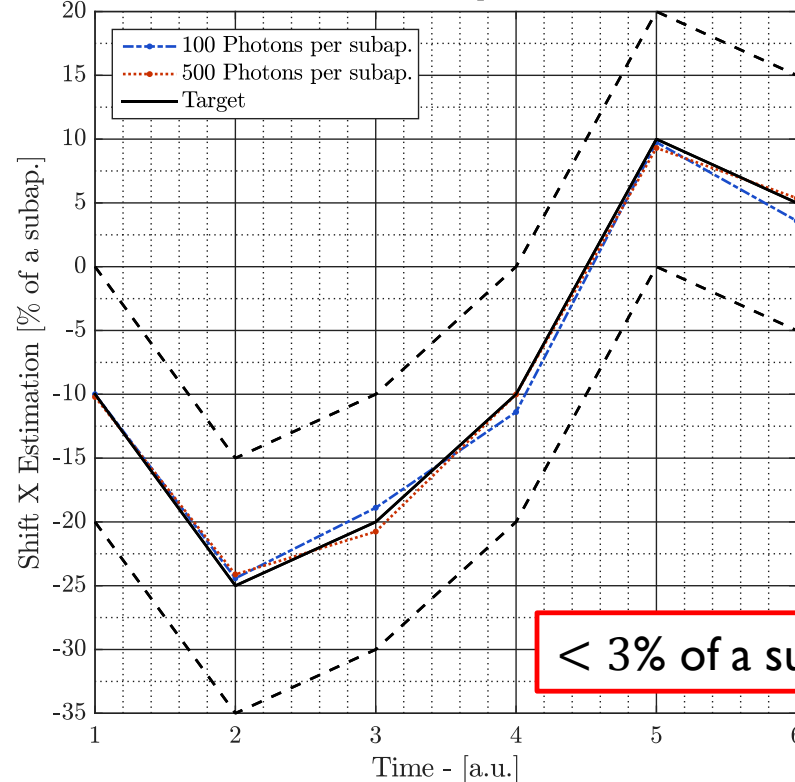
Rotation

3 PCA Modes - Amplitude: 20 nm



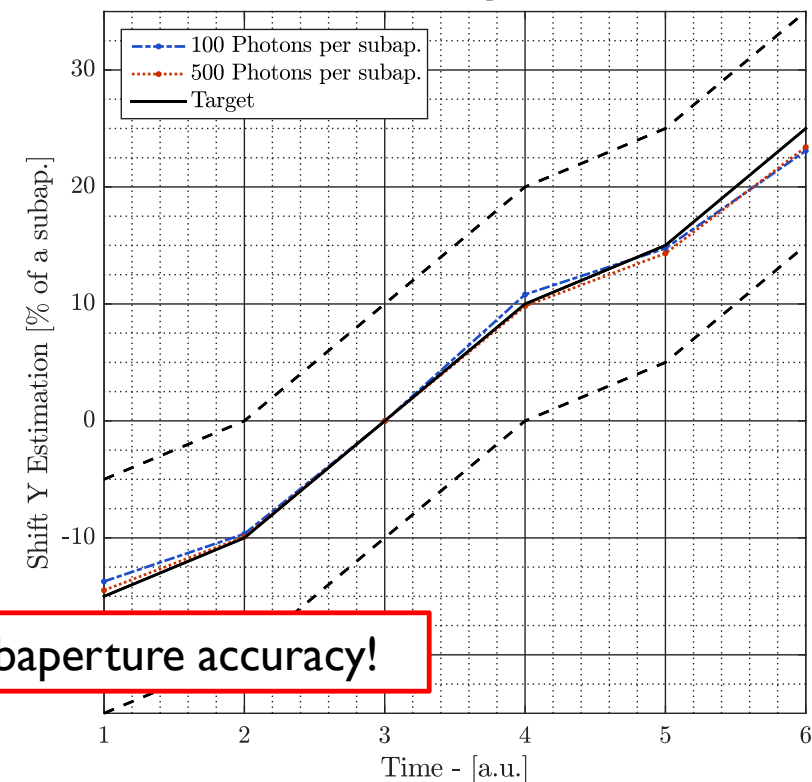
Shift X

3 PCA Modes - Amplitude: 20 nm



Shift Y

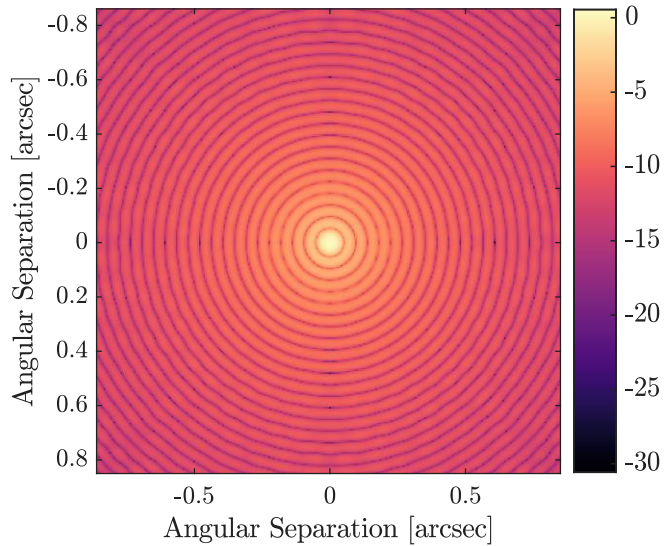
3 PCA Modes - Amplitude: 20 nm



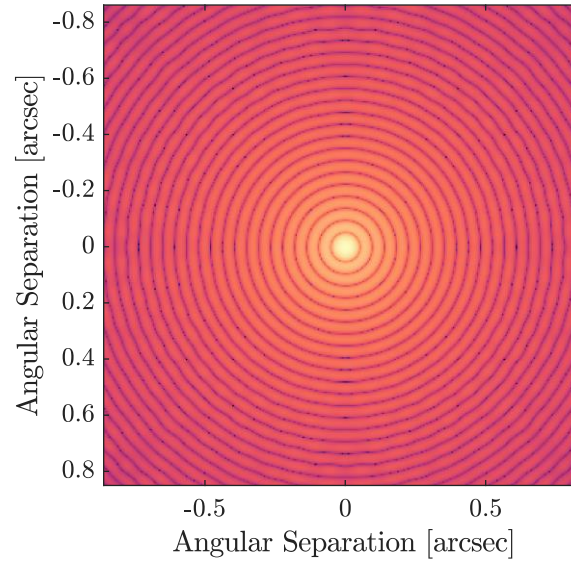
An Invasive Approach - Choice of the signals

Impact on the science path?

Diffraction-Limited PSF
(log scale)

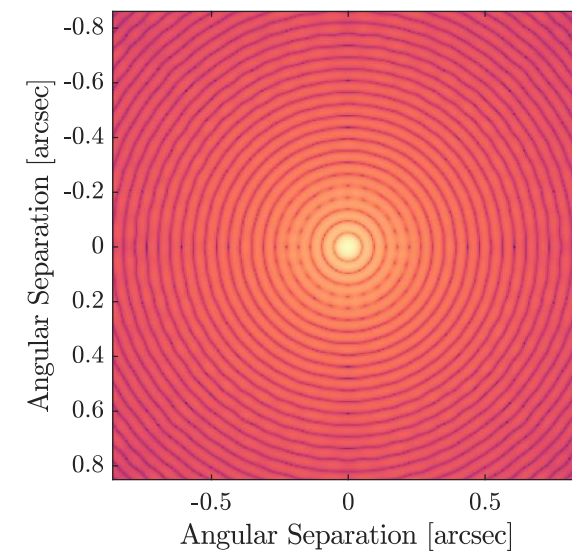


10 nm



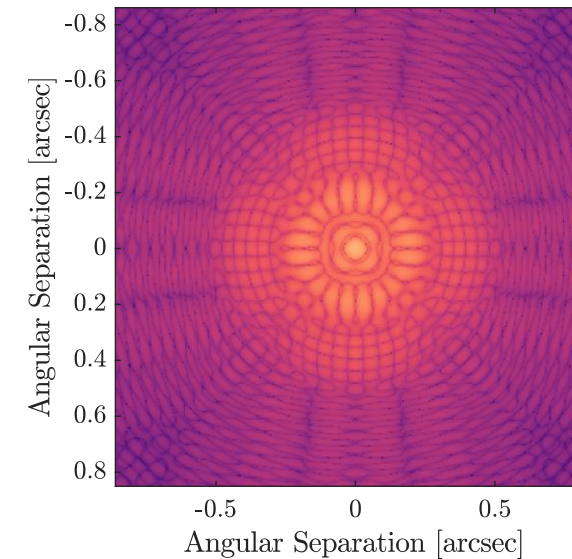
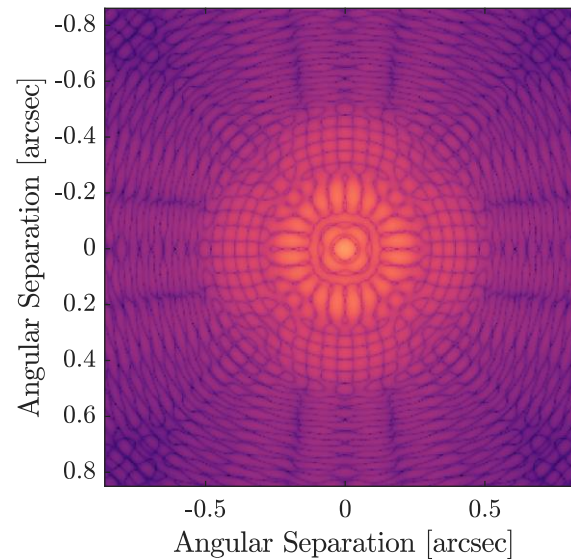
Max: 1e-6

20 nm



Max: 1e-4.6

PSF
(log scale)



Residual
PSF
(log scale)

An Invasive Approach

Advantages: Robustness and accuracy of the method!

Drawbacks: Impact on science has to be carefully evaluated

An Invasive Approach

Advantages: Robustness and accuracy of the method!

Drawbacks: Impact on science has to be carefully evaluated

High Contrast? => Non Invasive Approach

The Non-Invasive Approach - Principle

Principle:

- 1) Estimating an Interaction Matrix using the closed-loop data
- 2) Identification of the Mis-Registrations using this noisy Interaction Matrix

The Non-Invasive Approach - Principle

Principle:

I) Estimating an Interaction Matrix using the closed-loop data

AO – CL Equation

$$\begin{array}{c} \text{WFS Measurement Model} \quad \text{DM Command} \\ \downarrow \quad \downarrow \\ \text{WFS Measurement} \longrightarrow \mathbf{y}_k = \mathbf{M}_{\text{WFS}} \cdot \left(-\mathbf{M}_{\text{DM}\alpha} \cdot \mathbf{c}_k + \phi_k^{\text{turb}} \right) + \boldsymbol{\eta}_k \longleftarrow \text{Noise} \\ \uparrow \quad \uparrow \\ \text{DM Model} \quad \text{Turbulence} \end{array}$$

The Non-Invasive Approach - Principle

Principle:

1) Estimating an Interaction Matrix using the closed-loop data

AO – CL Equation

$$y_k = M_{WFS} \cdot (-M_{DM\alpha} \cdot c_k + \phi_k^{turb}) + \eta_k$$

Increments (Linearity + Independence of δc_k and $\delta \phi_k^{turb}$)

$$\delta y_k = -M_{WFS} \cdot M_{DM\alpha} \cdot \delta c_k + M_{WFS} \cdot \delta \phi_k^{turb} + \delta \eta_k$$

The Non-Invasive Approach - Principle

Principle:

1) Estimating an Interaction Matrix using the closed-loop data

AO – CL Equation

$$y_k = M_{WFS} \cdot (-M_{DM\alpha} \cdot c_k + \phi_k^{turb}) + \eta_k$$

Increments (Linearity + Independence of δc_k and $\delta \phi_k^{turb}$)

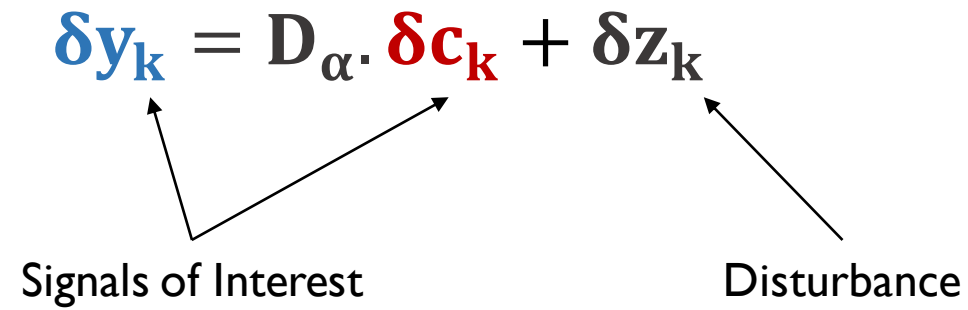
$$\delta y_k = \underbrace{-M_{WFS} \cdot M_{DM\alpha} \cdot \delta c_k}_{D_\alpha} + \underbrace{M_{WFS} \cdot \delta \phi_k^{turb} + \delta \eta_k}_{\text{Disturbance } \delta z_k}$$

The Non-Invasive Approach - Principle

Principle:

1) Estimating an Interaction Matrix using the closed-loop data

AO – CL Equation

$$\delta y_k = D_\alpha \cdot \delta c_k + \delta z_k$$


The diagram shows the equation $\delta y_k = D_\alpha \cdot \delta c_k + \delta z_k$. Below the equation, the text "Signals of Interest" has two arrows pointing to δy_k and δc_k . The text "Disturbance" has an arrow pointing to δz_k .

The Non-Invasive Approach - Principle

Principle:

I) Estimating an Interaction Matrix using the closed-loop data

AO – CL Equation

$$\delta y_k = D_\alpha \cdot \delta c_k + \delta z_k$$

Maximum Likelihood Approach:

$$D_\alpha = (C_{\delta y, \delta c}) \cdot (C_{\delta c, \delta c})^+$$

Covariance Covariance
Slopes/Commands Commands/Commands

The Non-Invasive Approach - Principle

Principle:

- 1) Estimating an Interaction Matrix using the closed-loop data
AO – CL Equation

$$\delta \mathbf{y}_k = \mathbf{D}_\alpha \cdot \delta \mathbf{c}_k + \delta \mathbf{z}_k$$

Maximum Likelihood Approach:

$$\mathbf{D}_\alpha = (\mathbf{C}_{\delta \mathbf{y}, \delta \mathbf{c}}) \cdot (\mathbf{C}_{\delta \mathbf{c}, \delta \mathbf{c}})^+$$

Hypothesis:

1. Independence between $\delta \mathbf{c}_k$ and $\delta \mathbf{z}_k$
 2. Perfect WFS
- Domain of validity? Limitations?

IV.2 - Analysis of the signals

$$\delta y_k = D_\alpha \cdot \delta c_k + \delta z_k$$

Signal of interest $\delta c_k \Rightarrow$ Propagation on the DM of :

- Noise Propagation
- Calibration Error
- Temporal Error
- Aliasing Error
- ...

IV.2 - Analysis of the signals

$$\delta y_k = D_\alpha \cdot \delta c_k + \delta z_k$$

Signal of interest $\delta c_k \Rightarrow$ Propagation on the DM of :

- Noise Propagation
 - Calibration Error
 - Temporal Error
 - Aliasing Error
 - ...
- Acts as a **signal of interest!**

IV.2 - Analysis of the signals

$$\delta y_k = D_\alpha \cdot \delta c_k + \delta z_k$$

Signal of interest $\delta c_k \Rightarrow$ Propagation on the DM of :

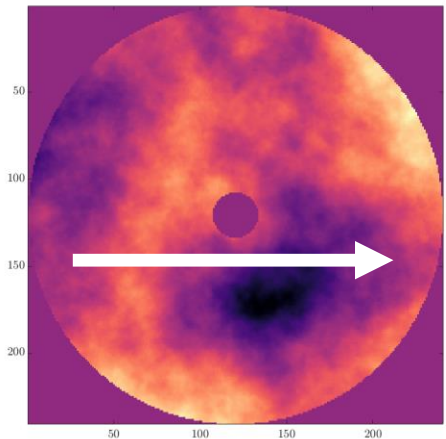
- Noise Propagation
- Calibration Error
- **Temporal Error**] — **Correlated** to the turbulence impacting the measurement!
- Aliasing Error
- ...

Challenging the hypothesis

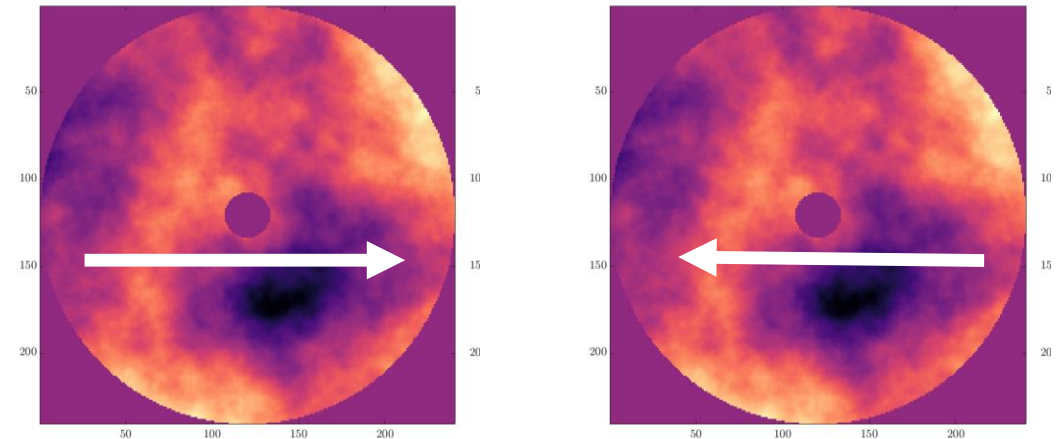
I. Independence between δc_k and δz_k ?

I. Explore different observing conditions : Frozen Flow and Boiling atmosphere

Frozen Flow



Boiling



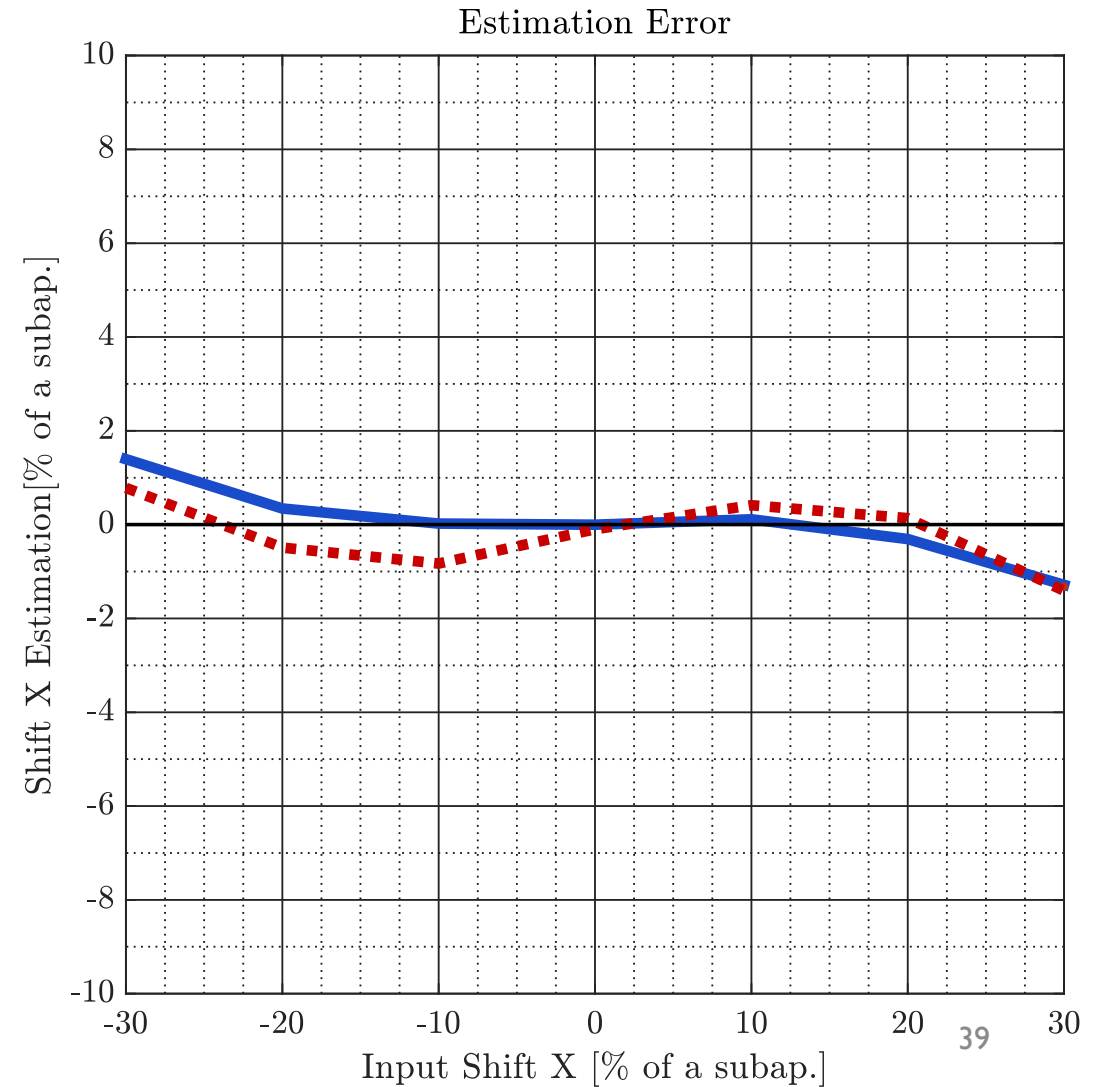
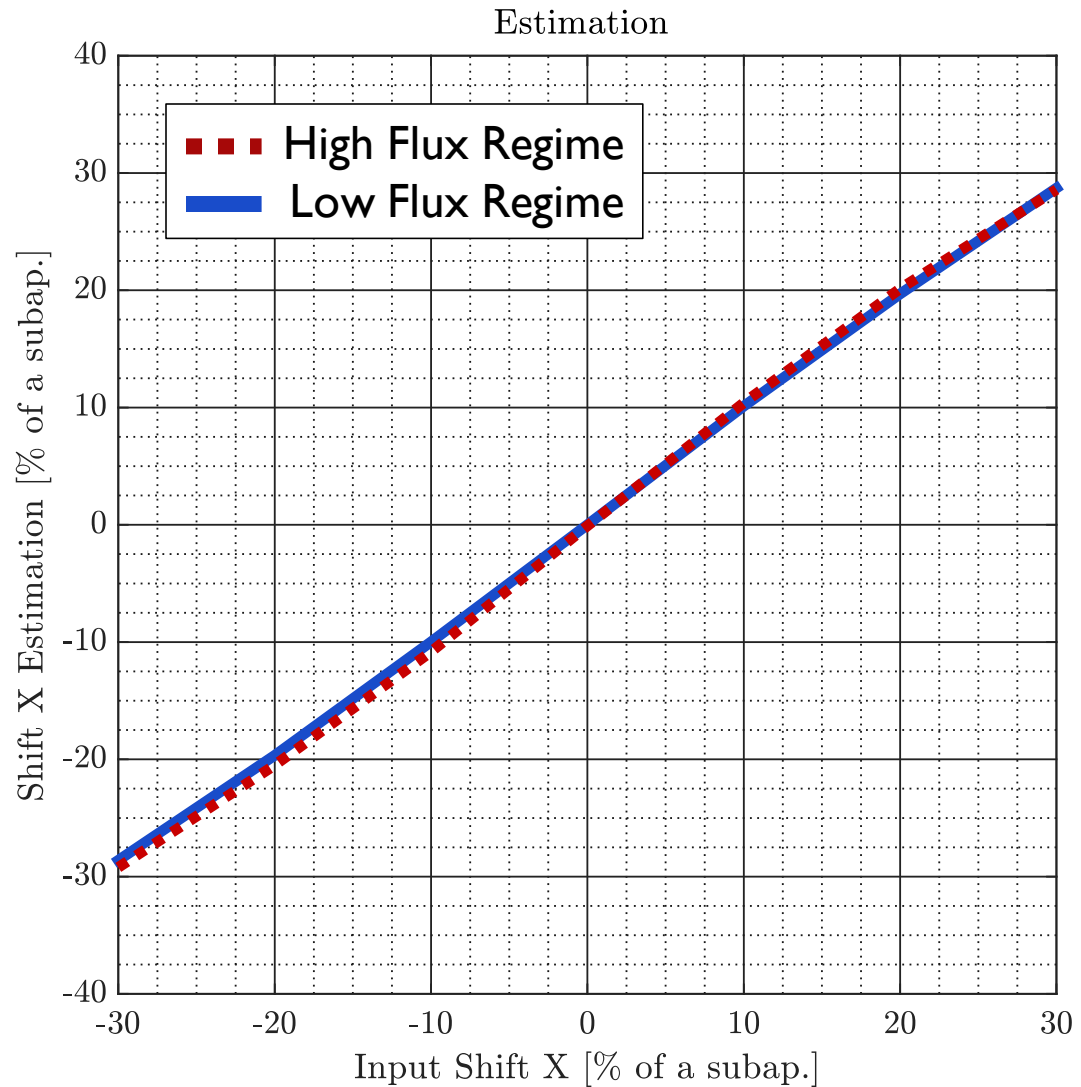
For both cases constant wind in the X direction

Challenging the hypothesis

1. Independence between δc_k and δz_k ?
 1. Explore different observing conditions : Frozen Flow and Boiling atmosphere
 2. Explore different regimes of noise

Application SH WFS

Nominal case: Frozen Flow 10 m/s X direction



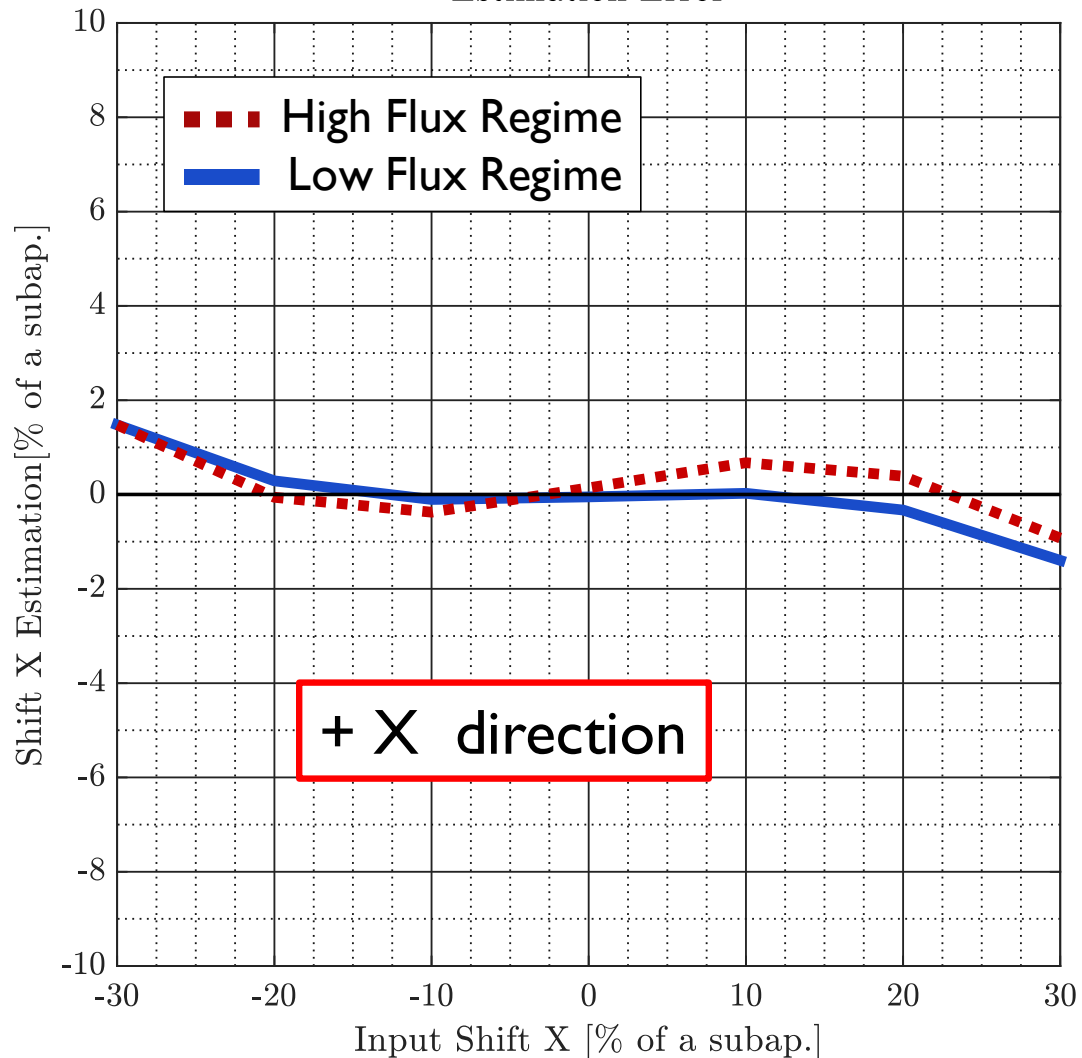
Application SH WFS

Nominal case: Frozen Flow

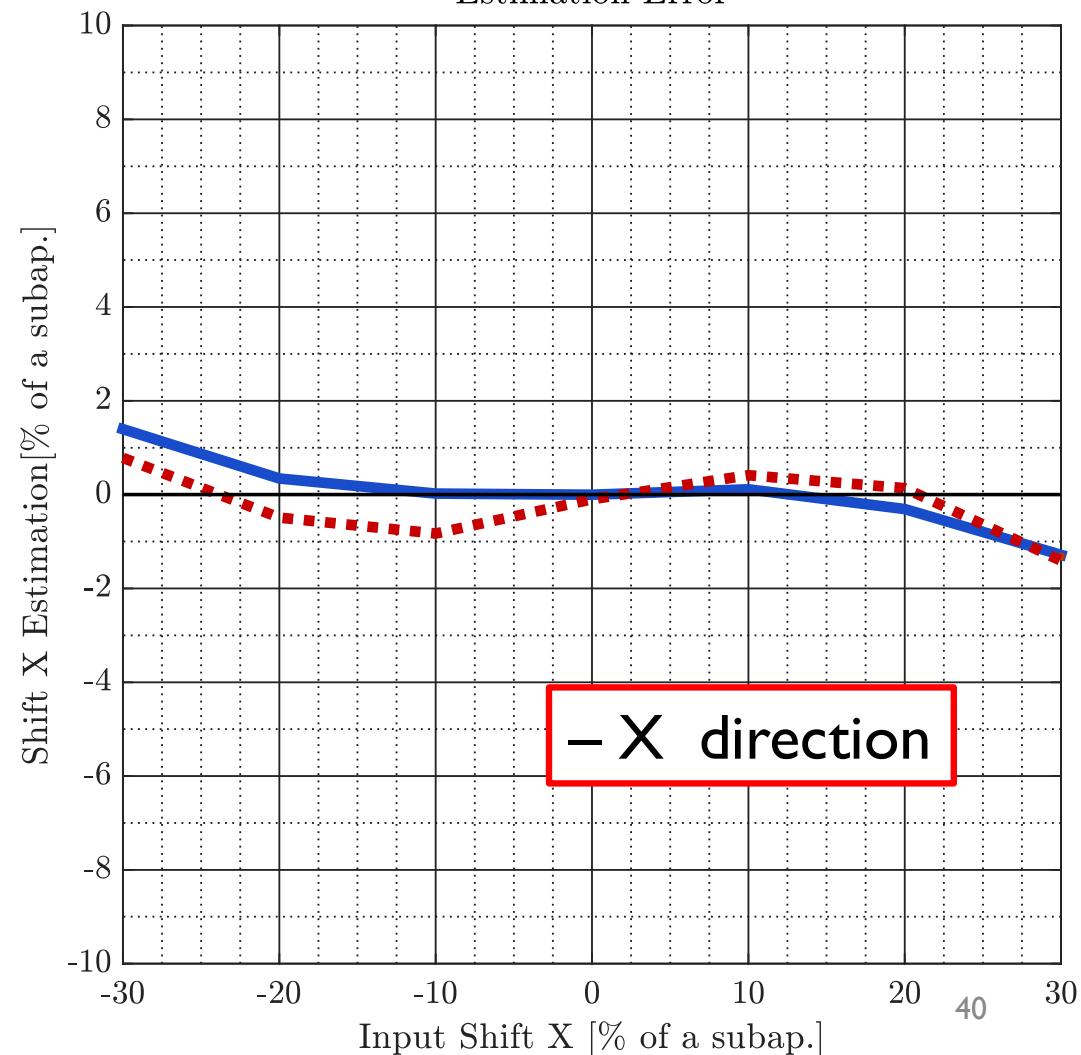
10 m/s

X direction

Estimation Error



Estimation Error



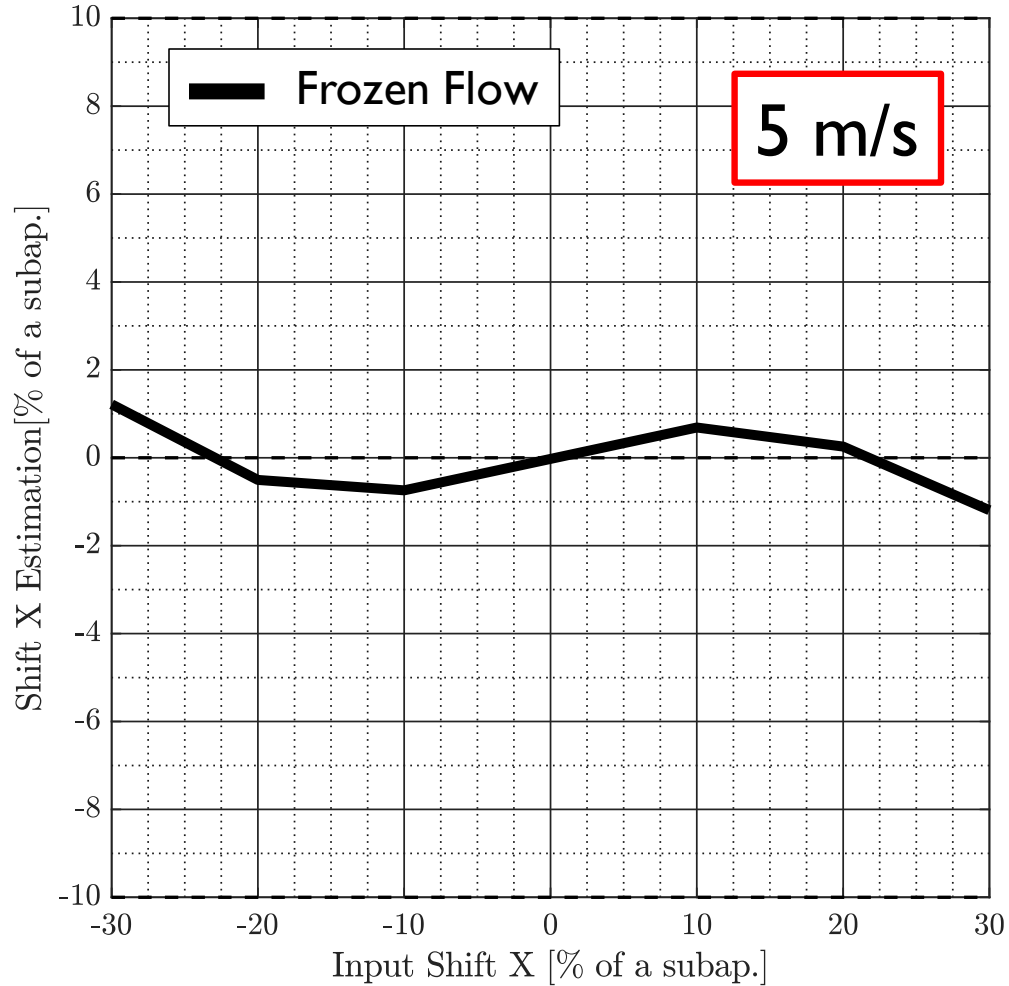
Application SH WFS

Limit cases:

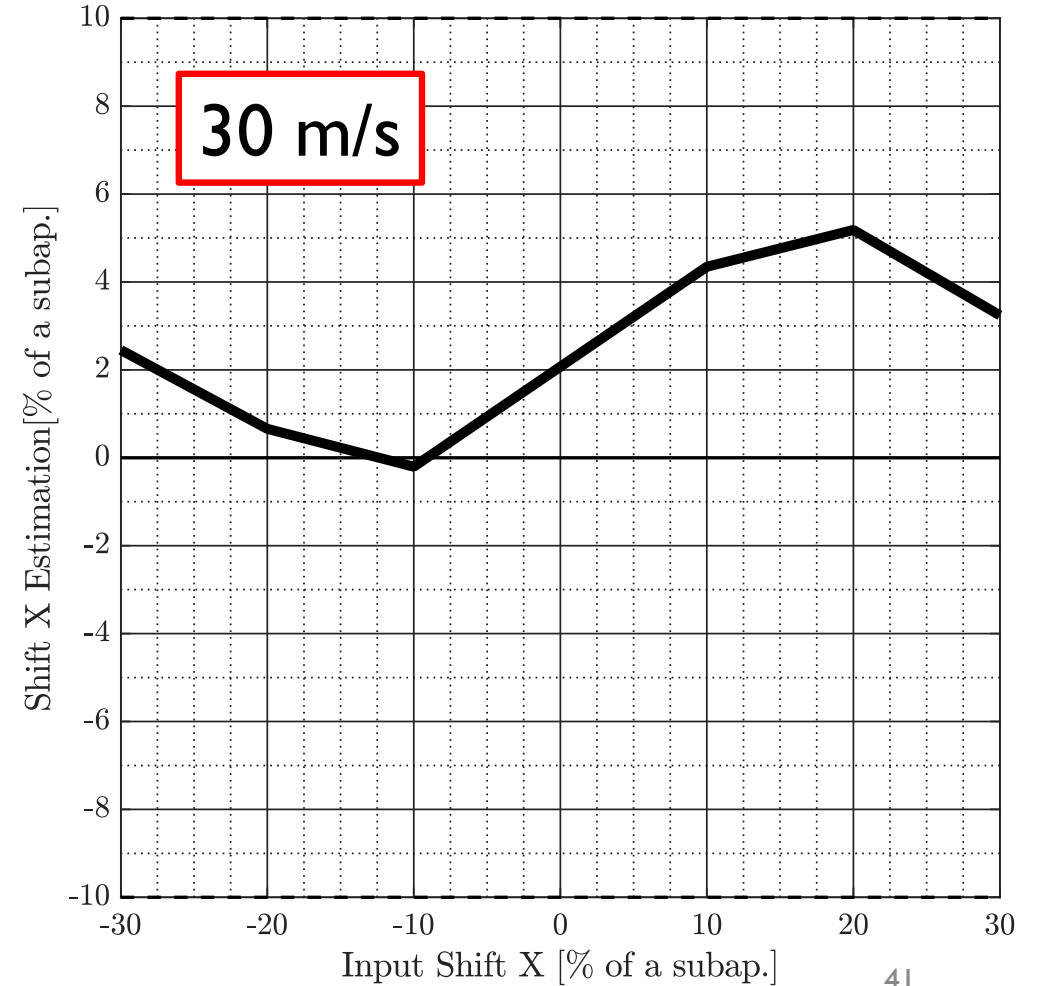
High Flux Regime

X Direction

Estimation Error



Estimation Error



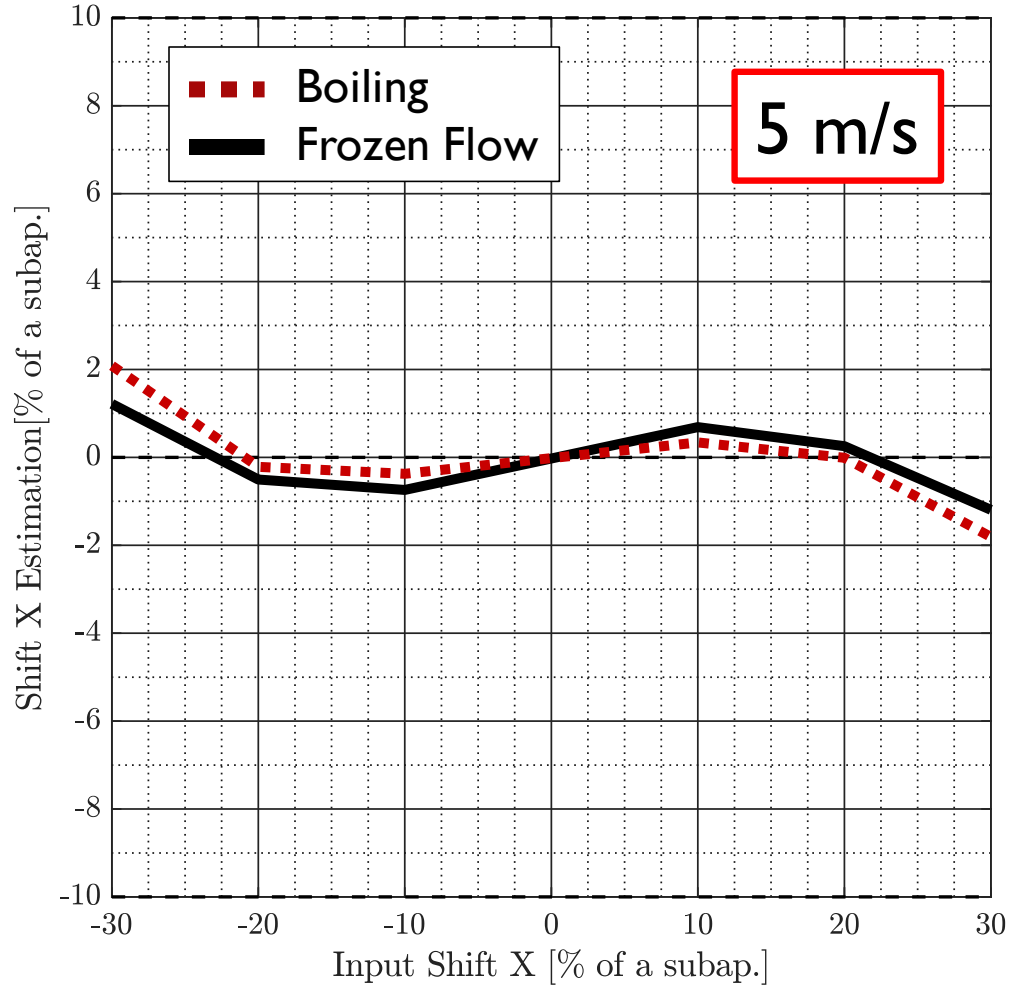
Application SH WFS

Limit cases:

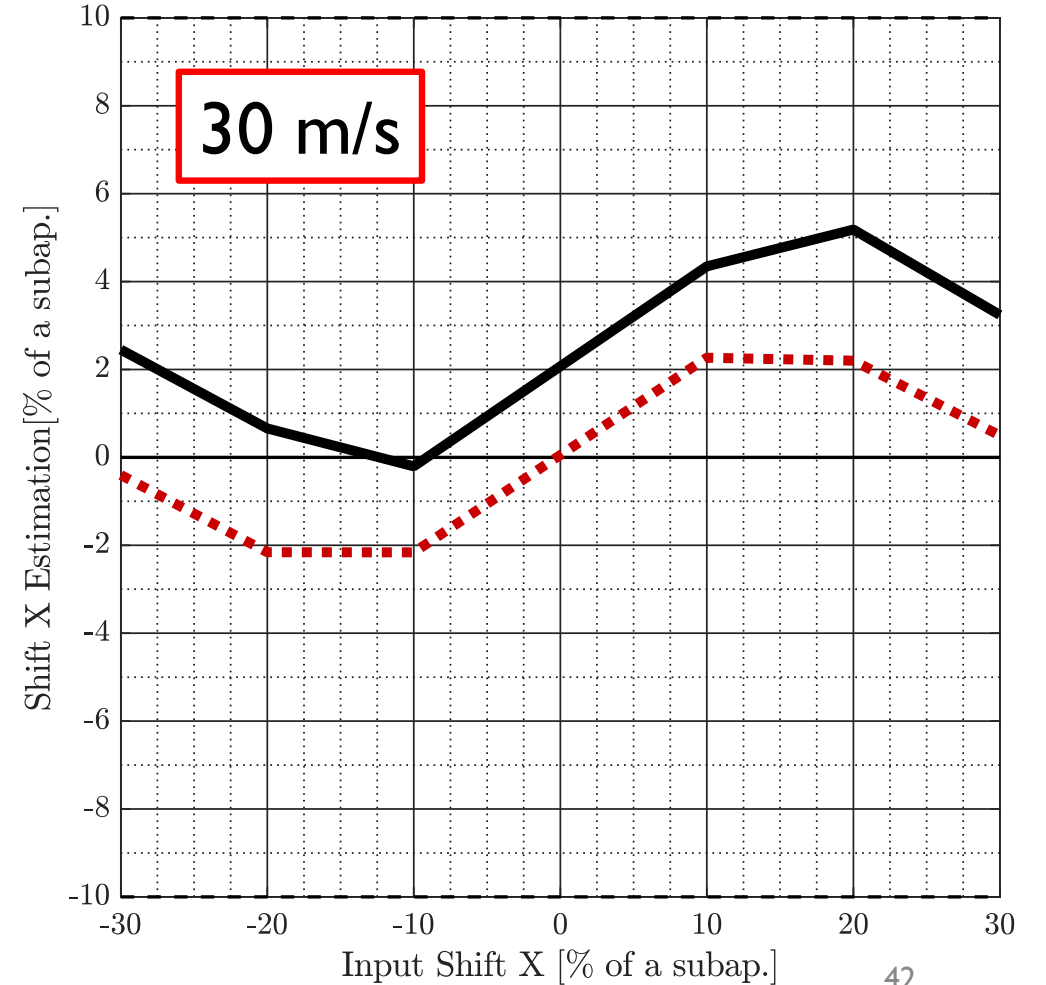
High Flux Regime

X Direction

Estimation Error



Estimation Error



Application SH WFS

Frozen Flow

Bias for the shift estimation!

- Depends on the wind speed
- Depends on the wind direction
- Depends on the regime of noise

Boiling

No bias for the shift estimation!

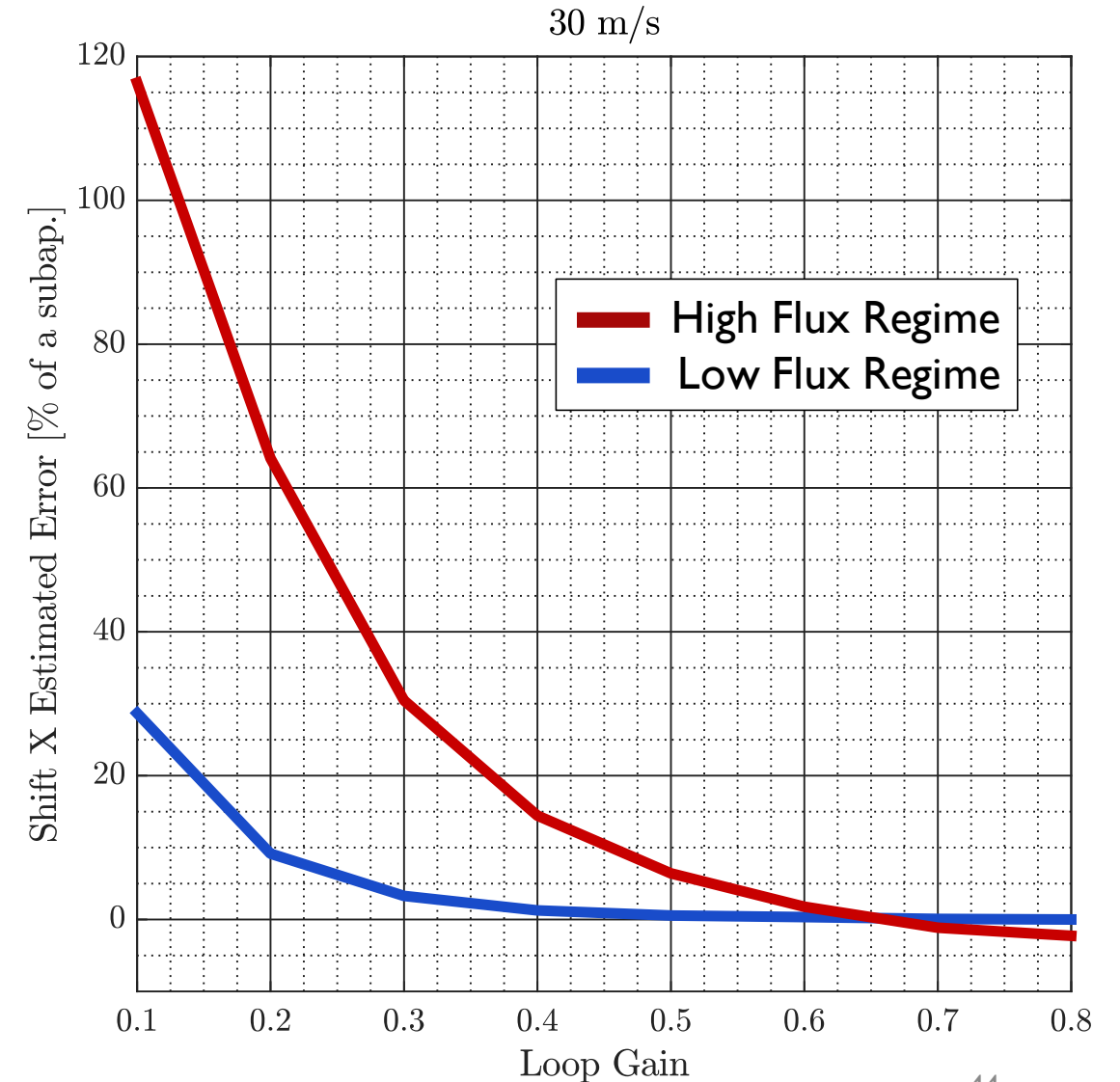
Application SH WFS

Problem comes from the Temporal Error..

Impact of the bandwidth?

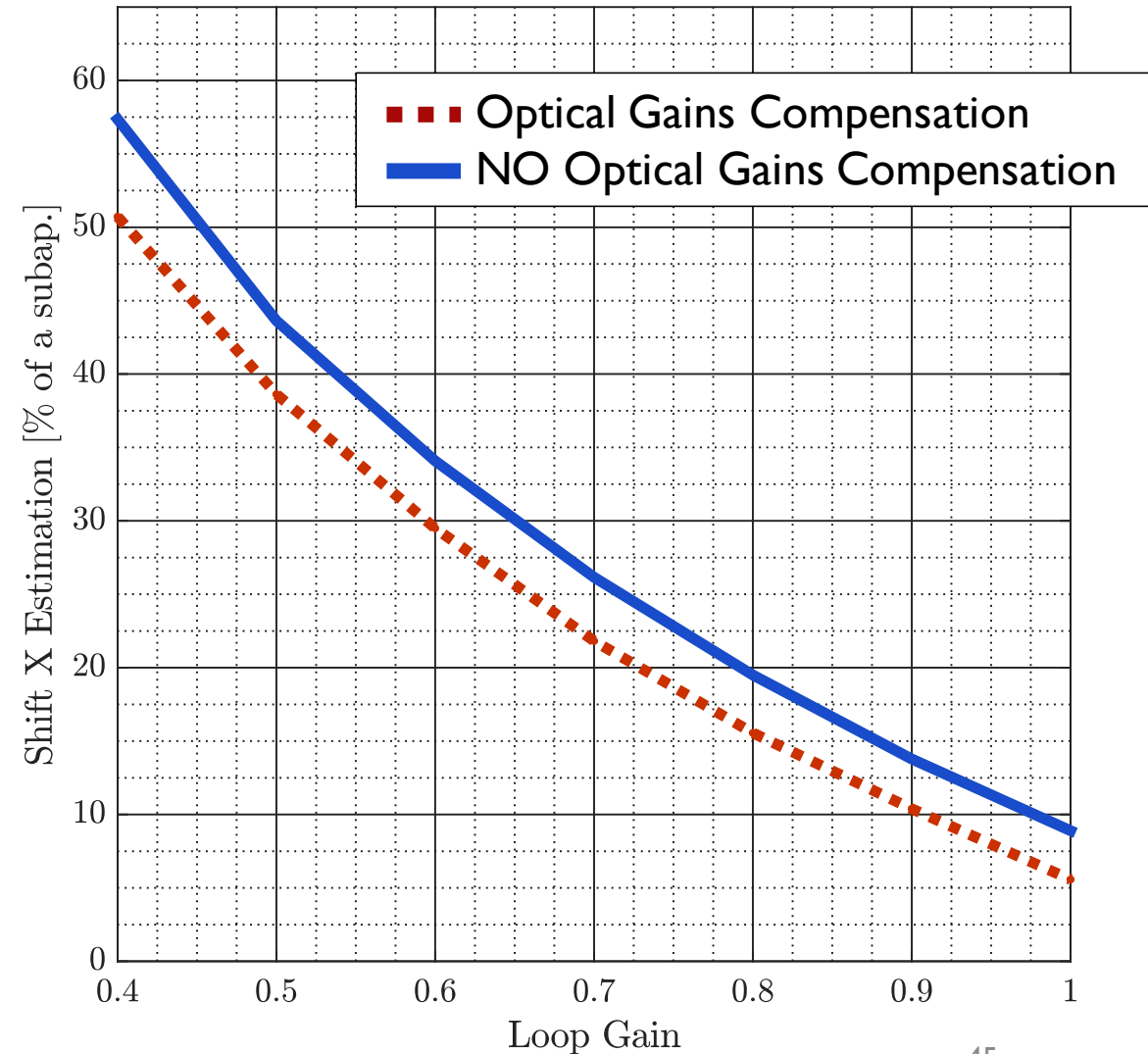
Bias correlated to the bandwidth!

=> Correction of the temporal error!



Application with PWFS

- Same Trends Identified!
- Higher impact of the bias:
- Optical Gains Compensations



A Non Invasive Approach

Summary:

Limitation of the method in a strong Frozen Flow and High Flux regime

BUT...We have to keep in mind that we considered:

- A pure Frozen Flow (constant wind speed and direction) => not so realistic
- Large Wind-speeds >20 m/s

Conclusions

AO Calibration in the ELT context

⇒ Pseudo Synthetic models to provide regular updates of the calibration

Invasive approach:

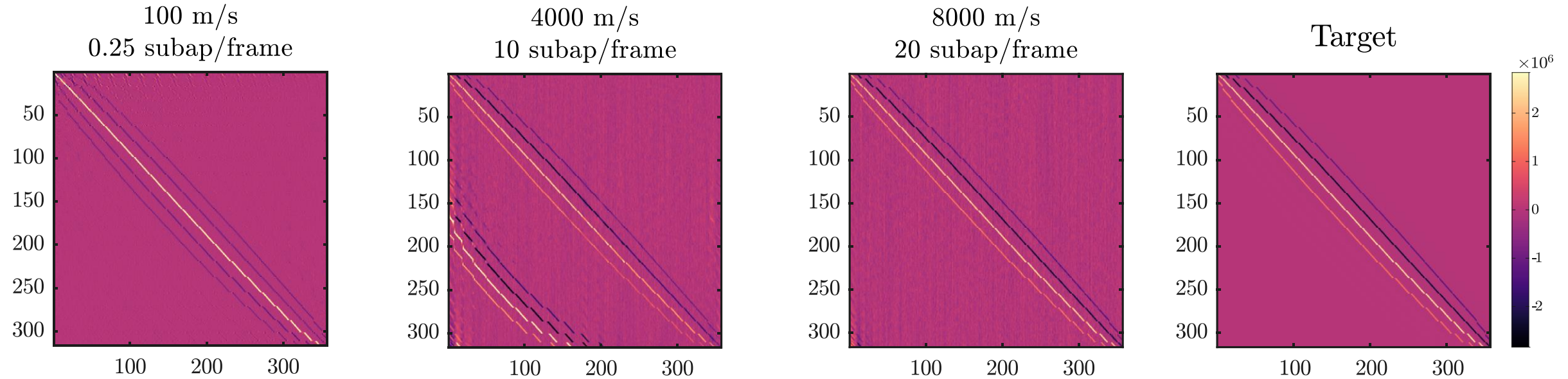
- Robust and behaving as we expect it to be.
- Impact on science

Non Invasive Approach

- NO impact on science
- Limitations in High Flux regime and Pure Frozen Flow ⇒ Priors?

Application SH WFS

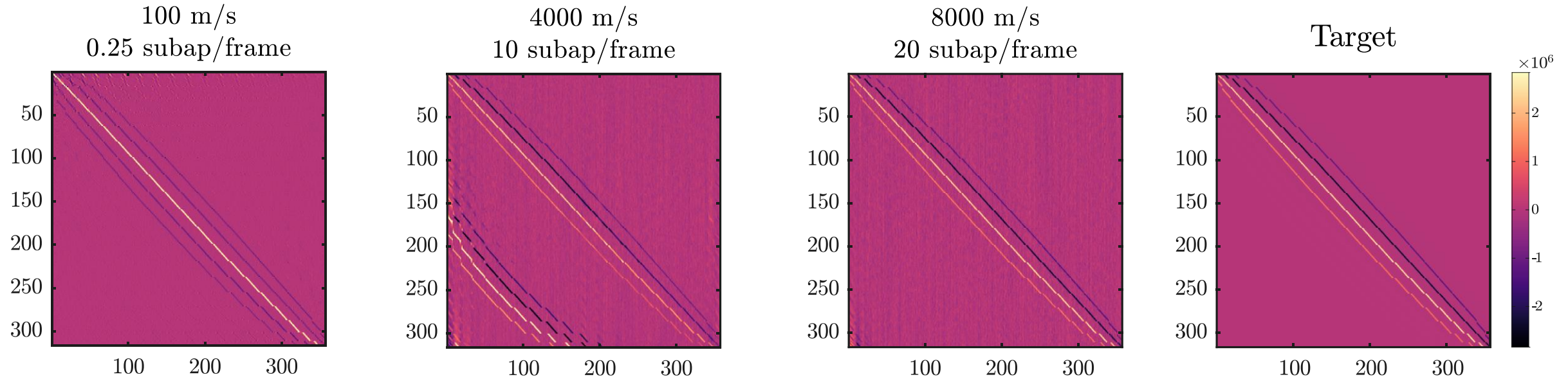
Origin of the Bias in High Flux Regime?



Structures in the interaction matrix estimation = replicas of actuators signals!

Application SH WFS

Origin of the Bias in High Flux Regime?



Structures in the interaction matrix estimation = replicas of actuators signals!

When overlapping with signal of interest => Bias the algorithm!

Identification Algorithm

Principle: Projection of an Interaction Matrix onto **Sensitivity Matrices**

Taylor's Development of the interaction matrix

$$\mathbf{D}_{\alpha} \approx \gamma \left(\mathbf{D}_{\alpha_0} + \sum_i \alpha_i \cdot \delta \mathbf{D}_{\alpha_0}(\varepsilon_i) \right)$$

\mathbf{D}_{α} = Input Interaction Matrix for mis-registration α

\mathbf{D}_{α_0} = Synthetic Interaction Matrix for mis-registration α_0

Identification Algorithm

Principle: Projection of an Interaction Matrix onto **Sensitivity Matrices**

Taylor's Development of the interaction matrix

$$\mathbf{D}_\alpha \approx \underset{\substack{\uparrow \\ \text{Scaling Factor}}}{\gamma} \left(\mathbf{D}_{\alpha_0} + \sum_i \alpha_i \cdot \underset{\substack{\downarrow \\ \text{Sensitivity Matrix}}}{\delta \mathbf{D}_{\alpha_0}(\varepsilon_i)} \right)$$

Mis-Registration parameter of type i

Sensitivity Matrix

$$\delta \mathbf{D}_{\alpha_0}(\varepsilon_i) = \frac{\mathbf{D}_{\alpha_0 + \varepsilon_i} - \mathbf{D}_{\alpha_0 - \varepsilon_i}}{2\varepsilon_i}$$

Identification Algorithm

Principle: Projection of an Interaction Matrix onto **Sensitivity Matrices**

Taylor's Development of the interaction matrix

$$\mathbf{D}_{\alpha} \approx \gamma \left(\mathbf{D}_{\alpha_0} + \sum_i \alpha_i \cdot \delta \mathbf{D}_{\alpha_0}(\varepsilon_i) \right)$$

Least Square Minimization:

Iterative Estimation of γ and α (A few iterations required)

⇒ All the mis-registration parameters identified simultaneously